

# Appendix B

# NSP Language Definition

## B.1 Context Free Grammar

```
string ::= s ∈ String  
id ::= l ∈ Label  
parameter-type ::= t ∈ T ∪ P  
supported-type ::= t ∈ Bsupported  
system ::= page | system system  
page ::= <nsp name="id"> websig-core </nsp>  
websig-core ::= param websig-core | webcall | include  
param ::= <param name="id" type="parameter-type" />  
webcall ::= <html> head body </html>  
head ::= <head><title> strings </title></head>  
strings ::= ε | string strings  
body ::= <body> dynamic </body>  
include ::= <include> dynamic </include>
```

```

dynamic ::=      dynamic dynamic
                   | ε | string
                   | ul | li
                   | table | tr | td
                   | call
                   | form | object | hidden | submit
                   | input | checkbox
                   | select | option
                   | expression
                   | code

ul ::= <ul> dynamic </ul>
li ::= <li> dynamic </li>

table ::= <table> dynamic </table>
tr ::= <tr> dynamic </tr>
td ::= <td> dynamic </td>

call ::= <call callee="id"> actualparams </call>

actualparams ::= εact | actualparam actualparams

actualparam ::= <actualparam param="id"> expr </actualparam>

form ::= <form callee="id"> dynamic </form>
object ::= <object param="id"> dynamic </object>
hidden ::= <hidden param="id"> expr </hidden>
submit ::= <submit/>
input ::= <input type="supported-type" param="id" />
checkbox ::= <checkbox param="id" />

```

```
select   ::=   <select param="id"> dynamic </select>  
option   ::=   <option>  
                  <value> expr </value>  
                  <label> expr </label>  
                </option>  
expression ::=   <expression> expr </expression>  
code     ::=   <code> com </code>  
com      ::=   </code> dynamic <code>  
                  | com ; com  
                  | if expr then com else com  
                  | while expr do com  
                  | stat  
stat    ::=   id := expr  
expr     ::=   id | expr.id | expr[expr]
```

## B.2 Types

### B.2.1 Programming Language Types

$$\mathbb{T} = \mathbb{B} \cup \mathbb{V} \cup \mathbb{A} \cup \mathbb{R} \cup \mathbb{Y}$$

$$(basic\ types) \quad \mathbb{B} = \mathbb{B}_{primitive} \cup \mathbb{B}_{supported}$$

$$(primitive\ basic\ types) \quad \mathbb{B}_{primitive} = \{\text{int}, \text{float}, \text{boolean}\}$$

$$(supported\ basic\ types) \quad \mathbb{B}_{supported} = \{\text{int}, \text{Integer}, \text{String}\}$$

$$(type\ variables) \quad \mathbb{V} = \begin{aligned} & \{X, Y, Z, \dots\} \\ & \cup \{\text{Person}, \text{Customer}, \text{Article}, \dots\} \end{aligned}$$

$$(array\ types) \quad \mathbb{A} = \{\text{array of } T \mid T \in \mathbb{T} \setminus \mathbb{A}\}$$

$$(record\ types) \quad \mathbb{R} = \text{Label} \dashrightarrow \mathbb{T}$$

$$(recursive\ types) \quad \mathbb{Y} = \{\mu X . R \mid X \in \mathbb{V}, R \in \mathbb{R}\}$$

### B.2.2 Server Page Types

$$(page\ types) \quad \mathbb{P} = \{w \rightarrow r \mid w \in \mathbb{W}, r \in \mathbb{C} \cup \mathbb{D}\}$$

$$(web\ signatures) \quad \mathbb{W} = \text{Label} \dashrightarrow (\mathbb{T} \cup \mathbb{P})$$

$$(complete\ web\ page) \quad \mathbb{C} = \{\square\}$$

$$(document\ fragment\ types) \quad \mathbb{D} = \mathbb{L} \times \mathbb{W}$$

$$(layout\ types) \quad \mathbb{L} = \mathbb{E} \times \mathbb{F}$$

$$(element\ types) \quad \mathbb{E} = \{\circ, \bullet, \text{TR}, \text{TD}, \text{LI}, \text{OP}\}$$

$$(form\ occurrences) \quad \mathbb{F} = \{\Downarrow, \Uparrow, \Updownarrow\}$$

$$(system\ types) \quad \mathbb{S} = \{\diamond, \checkmark\}$$

## B.3 Subtyping Relation

### B.3.1 Establishing Subtyping Rules

$$(reflexivity) \quad \frac{}{\vdash T < T}$$

$$(array\ types) \quad \frac{}{\vdash T < \text{array of } T}$$

$$\left( \begin{array}{l} \text{record types} \\ \text{web signatures} \end{array} \right) \quad \frac{T_j \notin \mathbb{B}_{\text{primitive}} \cup \mathbb{P} \quad j \in 1 \dots n}{\vdash \{l_i \mapsto T_i\}_{i \in 1 \dots j-1, j+1 \dots n} < \{l_i \mapsto T_i\}_{i \in 1 \dots n}}$$

$$(html\ types) \quad \frac{T \in \mathbb{E}}{\vdash \circ < T}$$

$$(form\ occurrences) \quad \frac{T \in \mathbb{F}}{\vdash \ddagger < T}$$

### B.3.2 Preserving Subtyping Rules

$$(array\ types) \quad \frac{\vdash S < T}{\vdash \text{array of } S < \text{array of } T}$$

$$\left( \begin{array}{l} \text{record types} \\ \text{web signatures} \end{array} \right) \quad \frac{\vdash S_1 < T_1 \dots \vdash S_n < T_n}{\vdash \{l_i \mapsto S_i\}_{i \in 1 \dots n} < \{l_i \mapsto T_i\}_{i \in 1 \dots n}}$$

$$(recursive\ types) \quad \frac{\vdash S[\mu X.S/X] < T \quad \vdash S < T[\mu X.T/X]}{\vdash \mu X.S < T \quad \vdash S < \mu X.T}$$

$$(page\ types) \quad \frac{\vdash w' < w \quad \vdash R < R'}{\vdash w \rightarrow R < w' \rightarrow R'}$$

$$\left( \begin{array}{l} \text{dynamic} \\ \text{layout types} \end{array} \right) \quad \frac{\vdash S_1 < T_1 \quad \vdash S_2 < T_2}{\vdash (S_1, S_2) < (T_1, T_2)}$$

## B.4 Type Operators

$$\underline{-}^* : T \rightarrow T$$

$$T^* \equiv_{\text{DEF}} \begin{cases} \text{array of } T & , T \notin \mathbb{A} \\ T & , \text{else} \end{cases}$$

$$\underline{\phantom{W}} \odot \underline{\phantom{W}} : W \multimap W$$

$$w_1 \odot w_2 \equiv_{\text{DEF}}$$

$$\left\{ \begin{array}{l} \perp , \textbf{if } \exists(l_1 \mapsto T_1) \in w_1 \bullet \exists(l_2 \mapsto T_2) \in w_2 \bullet l_1 = l_2 \wedge P_1 \in \mathbb{P} \wedge P_2 \in \mathbb{P} \\ \perp , \textbf{if } \exists(l_1 \mapsto T_1) \in w_1 \bullet \exists(l_2 \mapsto T_2) \in w_2 \bullet l_1 = l_2 \wedge T_1 \sqcup T_2 \text{ undefined} \\ \\ (\text{dom } w_2) \triangleleft w_1 \cup (\text{dom } w_1) \triangleleft w_2 \\ \cup \quad \{ (l \mapsto (T_1 \sqcup T_2)*) \mid (l \mapsto T_1) \in w_1 \wedge (l \mapsto T_2) \in w_2 \} \end{array} \right. , \textbf{else}$$

## B.5 Environments and Judgements

$$\Gamma : \mathbf{Label} \dashv\vdash (\mathbb{T} \cup \mathbb{P}) = \mathbb{W} \quad (identifiers)$$

$\Delta : \mathbf{Label} \dashv\vdash \mathbb{P} \subset \mathbb{W}$  (page definitions)

$$\Gamma \vdash e : \mathbb{T} \cup \mathbb{P} \quad e \in \mathbf{expr}$$

$$\Gamma \vdash n : \mathbb{D} \quad n \in \mathbf{com} \cup \mathbf{dynamic}$$

$\Gamma \vdash c : \mathbb{P}$        $c \in \text{websig-core}$

$\Gamma \vdash a : \mathbb{W}$        $a \in \text{actualparams}$

$\Gamma, \Delta \vdash s : \mathbb{S}$        $s \in \text{system}$

## B.6 Typing Rules

$$\frac{\begin{array}{c} \Gamma \in \mathbb{R} \\ (\text{dom } \Delta) \cap \text{bound}(s) = \emptyset \\ \Gamma, \Delta \vdash s : \diamond \end{array}}{\Gamma, \Delta \vdash s : \checkmark} \quad (\text{B.1})$$

$$\frac{\begin{array}{c} s_1, s_2 \in \mathbf{system} \quad (\text{dom } \Delta_1) \cap (\text{dom } \Delta_2) = \emptyset \\ ((\text{dom } \Gamma_2) \triangleleft \Delta_1) < ((\text{dom } \Delta_1) \triangleleft \Gamma_2) \\ ((\text{dom } \Gamma_1) \triangleleft \Delta_2) < ((\text{dom } \Delta_2) \triangleleft \Gamma_1) \\ \Gamma_1, \Delta_1 \vdash s_1 : \diamond \quad \Gamma_2, \Delta_2 \vdash s_2 : \diamond \end{array}}{((\text{dom } \Delta_2) \triangleleft \Gamma_1) \cup ((\text{dom } \Delta_1) \triangleleft \Gamma_2), \Delta_1 \cup \Delta_2 \vdash s_1 s_2 : \diamond} \quad (\text{B.2})$$

$$\frac{\Gamma \vdash l : P \quad \Gamma \vdash c : P \quad c \in \mathbf{websig-core}}{\Gamma \setminus (l \mapsto P), \{(l \mapsto P)\} \vdash < \mathbf{nsp} \mathbf{name} = "l" > c < / \mathbf{nsp} > : \diamond} \quad (\text{B.3})$$

$$\frac{\Gamma \vdash l : T \quad \Gamma \vdash c : w \rightarrow D \quad l \notin (\text{dom } w)}{\Gamma \setminus (l \mapsto T) \vdash < \mathbf{param} \mathbf{name} = "l" \mathbf{type} = "T" / > c : (w \cup \{(l \mapsto T)\}) \rightarrow D} \quad (\text{B.4})$$

$$\frac{\begin{array}{c} \Gamma \vdash d : ((\bullet \vee \circ, \Downarrow \vee \Uparrow), \emptyset) \quad t \in \mathbf{strings} \quad d \in \mathbf{dynamic} \\ < \mathbf{html} > \\ \Gamma \vdash < \mathbf{head} > < \mathbf{title} > t < / \mathbf{head} > < / \mathbf{title} > \\ < \mathbf{body} > d < / \mathbf{body} > \\ < / \mathbf{html} > : \emptyset \rightarrow \square \end{array}}{\Gamma \vdash < \mathbf{include} > d < / \mathbf{include} > : \emptyset \rightarrow D} \quad (\text{B.5})$$

$$\frac{\Gamma \vdash d : D \quad d \in \mathbf{dynamic}}{\Gamma \vdash < \mathbf{include} > d < / \mathbf{include} > : \emptyset \rightarrow D} \quad (\text{B.6})$$

$$\frac{d \in \mathbf{string}}{\Gamma \vdash d : ((\bullet, \Downarrow), \emptyset)} \quad (\text{B.7})$$

$$\frac{}{\Gamma \vdash \varepsilon : ((\circ, \Downarrow), \emptyset)} \quad (\text{B.8})$$

$$\frac{\begin{array}{c} d_1, d_2 \in \mathbf{dynamic} \\ \Gamma \vdash d_1 : (L_1, w_1) \quad \Gamma \vdash d_2 : (L_2, w_2) \quad L_1 \sqcup L_2 \downarrow \quad w_1 \odot w_2 \downarrow \end{array}}{\Gamma \vdash d_1 d_2 : (L_1 \sqcup L_2, w_1 \odot w_2)} \quad (\text{B.9})$$

$$\frac{\Gamma \vdash d : ((\mathbf{LI} \vee \circ, F), w)}{< \mathbf{ul} > d < / \mathbf{ul} > : ((\bullet, F), w)} \quad (\text{B.10})$$

$$\frac{\Gamma \vdash d : ((\bullet \vee \circ, F), w)}{< \mathbf{li} > d < / \mathbf{li} > : ((\mathbf{LI}, F), w)} \quad (\text{B.11})$$

$$\frac{\Gamma \vdash d : ((\mathbf{TR} \vee \circ, F), w)}{< \mathbf{table} > d < / \mathbf{table} > : ((\bullet, F), w)} \quad (\text{B.12})$$

$$\frac{\Gamma \vdash d : ((\mathbf{TD} \vee \circ, F), w)}{< \mathbf{tr} > d < / \mathbf{tr} > : ((\mathbf{TR}, F), w)} \quad (\text{B.13})$$

$$\frac{\Gamma \vdash d : ((\bullet \vee \circ, F), w)}{< \mathbf{td} > d < / \mathbf{td} > : ((\mathbf{TD}, F), w)} \quad (\text{B.14})$$

$$\frac{\Gamma \vdash l : w \rightarrow D \quad \Gamma \vdash as : v \quad \vdash v < w}{\Gamma \vdash < \mathbf{call} \mathbf{callee} = "l" > as < / \mathbf{call} > : D} \quad (\text{B.15})$$

$$\frac{}{\Gamma \vdash \varepsilon_{\mathbf{act}} : \emptyset} \quad (\text{B.16})$$

$$\frac{\Gamma \vdash as : w \quad \Gamma \vdash e : T \quad l \notin (dom w)}{\Gamma \vdash < \mathbf{actualparam} \mathbf{param} = "l" > as : w \cup \{(l \mapsto T)\}} \quad (\text{B.17})$$

$$\frac{\Gamma \vdash l : w \rightarrow \square \quad \Gamma \vdash d : ((e, \Downarrow), v) \quad \vdash v < w}{\Gamma \vdash < \mathbf{form} \mathbf{callee} = "l" > d < / \mathbf{form} > : ((e, \Uparrow), \emptyset)} \quad (\text{B.18})$$

$$\frac{\Gamma \vdash d : (L, w)}{\Gamma \vdash < \mathbf{object} \mathbf{param} = "l" > d < / \mathbf{object} > : (L, \{(l \mapsto w)\})} \quad (\text{B.19})$$

$$\frac{\Gamma \vdash e : T}{\Gamma \vdash < \mathbf{hidden} \mathbf{param} = "l" > e < / \mathbf{hidden} > : ((\circ, \Downarrow), \{(l \mapsto T)\})} \quad (\text{B.20})$$

$$\frac{}{\Gamma \vdash < \mathbf{submit} > : ((\bullet, \Downarrow), \emptyset)} \quad (\text{B.21})$$

$$\frac{T \in \mathbb{B}_{supported}}{\Gamma \vdash \text{< input type = "T" param = "l" / >} : ((\bullet, \Downarrow), \{(l \mapsto T)\})} \quad (\text{B.22})$$

$$\frac{}{\Gamma \vdash \text{< checkbox param = "l" / >} : ((\bullet, \Downarrow), \{(l \mapsto \text{boolean})\})} \quad (\text{B.23})$$

$$\frac{\begin{array}{c} \Gamma \vdash d : ((\mathbf{OP}, \Downarrow), \{(l \mapsto \text{array of } T)\}) \\ \text{< select param = "l" / >} \end{array}}{\Gamma \vdash \frac{d}{\text{/select}} : ((\bullet, \Downarrow), \{(l \mapsto \text{array of } T)\})} \quad (\text{B.24})$$

$$\frac{\begin{array}{c} \Gamma \vdash v : T \quad \Gamma \vdash e : S \quad S \in \mathbb{B} \quad l \in \mathbf{Label} \\ \text{< option / >} \end{array}}{\Gamma \vdash \frac{\begin{array}{c} \text{< value / >} v \quad \text{< label / >} e \\ \text{< /label / >} \end{array}}{\text{/option}} : ((\mathbf{OP}, \Downarrow), \{(l \mapsto \text{array of } T)\})} \quad (\text{B.25})$$

$$\frac{\Gamma \vdash e : T \quad T \in \mathbb{B}}{\Gamma \vdash \text{< expression / >} e \text{ < /expression / >} : ((\bullet, \Downarrow), \emptyset)} \quad (\text{B.26})$$

$$\frac{\Gamma \vdash c : D}{\Gamma \vdash \text{< code / >} c \text{ < /code / >} : D} \quad (\text{B.27})$$

$$\frac{\Gamma \vdash d : D}{\Gamma \vdash \text{< /code / >} d \text{ < code / >} : D} \quad (\text{B.28})$$

$$\frac{\Gamma \vdash c_1 : (L_1, w_1) \quad \Gamma \vdash c_2 : (L_2, w_2) \quad L_1 \sqcup L_2 \downarrow \quad w_1 \odot w_2 \downarrow}{\Gamma \vdash c_1; c_2 : (L_1 \sqcup L_2, w_1 \odot w_2)} \quad (\text{B.29})$$

$$\frac{\Gamma \vdash e : \text{boolean} \quad \Gamma \vdash c_1 : D_1 \quad \Gamma \vdash c_2 : D_2 \quad D_1 \sqcup D_2 \downarrow}{\Gamma \vdash \text{if } e \text{ then } c_1 \text{ else } c_2 : D_1 \sqcup D_2} \quad (\text{B.30})$$

$$\frac{\Gamma \vdash e : \text{boolean} \quad \Gamma \vdash c : (L, w)}{\Gamma \vdash \text{while } e \text{ do } c : (L, w \odot w)} \quad (\text{B.31})$$

$$\frac{\Gamma \vdash x : T \quad \Gamma \vdash e : T \quad T \in \mathbb{T}}{\Gamma \vdash x := e : ((\circ, \Downarrow), \emptyset)} \quad (\text{B.32})$$

$$\frac{(v \mapsto T) \in \Gamma}{\Gamma \vdash v : T} \quad (\text{B.33})$$

$$\frac{\Gamma \vdash e : \{l_i \mapsto T_i\}^{i \in 1 \dots n} \quad j \in 1 \dots n}{\Gamma \vdash e.l_j : T_j} \quad (\text{B.34})$$

$$\frac{\Gamma \vdash e : \text{array of } T \quad \Gamma \vdash i : \text{int}}{\Gamma \vdash e[i] : T} \quad (\text{B.35})$$

## B.7 Example Type Derivation I

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**Listing B.1**

---

```

01 <nsp name="A">
02   <param name="x" type="array of int"/>
03   <include> ε </include>
04 </nsp>
05
06 <nsp name="B">
07   <param name="x" type="int"/>
08   <include>
09     <li>
10       <expression> x </expression>
11     </li>
12   </include>
13 </nsp>
14
15 <nsp name="C">
16   <param name="p" type="((x ↦ int) → ((LI, ⇧), ∅))"/>
17   <include>
18     <call callee="p">
19       <actualparam param="x"> 815 </actualparam>
20     </call>
21   </include>
22 </nsp>
23
24 <nsp name="D">
25   <html>
26     <head><title> Main Page </title></head>
27     <body>
28       <ul>
29         <call callee="C">
30           <actualparam param="p"> A </actualparam>
31         </call>
32         <call callee="C">
33           <actualparam param="p"> B </actualparam>
34         </call>
35       </ul>
36     </body>
37   </html>
38 </nsp>
```

---

$$\Gamma_{CONST} \equiv_{DEF} \{815 \mapsto \text{int}\}$$

$$w_A \equiv_{DEF} \{(x \mapsto \text{array of int})\}$$

$$\Gamma_A \equiv_{DEF} \Gamma_{CONST} \cup \Delta_A \cup w_A$$

$$T_A \equiv_{DEF} w_A \rightarrow ((\circ, \ddagger), \emptyset)$$

$$\Delta_A \equiv_{DEF} \{(A \mapsto T_A)\}$$

$$w_B \equiv_{DEF} \{(x \mapsto \text{int})\}$$

$$\Gamma_B \equiv_{DEF} \Gamma_{CONST} \cup \Delta_B \cup w_B$$

$$T_B \equiv_{DEF} w_B \rightarrow ((LI, \ddagger), \emptyset)$$

$$\Delta_B \equiv_{DEF} \{(B \mapsto T_B)\}$$

$$w_C \equiv_{DEF} \{(p \mapsto T_B)\}$$

$$\Gamma_C \equiv_{DEF} \Gamma_{CONST} \cup \Delta_C \cup w_C$$

$$\Delta_C \equiv_{DEF} \{(C \mapsto (w_C \rightarrow ((LI, \ddagger), \emptyset)))\}$$

$$\Gamma_D^{FINAL} \equiv_{DEF} \Gamma_{CONST} \cup \Delta_A \cup \Delta_B \cup \Delta_C$$

$$\Gamma_D \equiv_{DEF} \Gamma_D^{FINAL} \cup \Delta_D$$

$$\Delta_D \equiv_{DEF} \{(\ D \mapsto (\emptyset \rightarrow \square))\}$$

$$\text{I} \quad \Gamma_A \vdash \varepsilon : ((\circ, \ddagger), \emptyset) \qquad \qquad \qquad \text{B.8}$$

$$\text{II} \quad \Gamma_A \vdash 03:\emptyset \rightarrow ((\circ, \ddagger), \emptyset) \qquad \qquad \qquad \text{I B.6}$$

$$\text{III} \quad \Gamma_A \vdash \text{x:array of int} \qquad \qquad \qquad \text{B.33}$$

$$\text{IV} \quad \Gamma_A \setminus w_A \vdash 02-03:T_A \qquad \qquad \qquad \text{III II B.4}$$

$$\text{V} \quad \Gamma_A \setminus w_A \vdash A : T_A \qquad \qquad \qquad \text{B.33}$$

$$\text{VI} \quad \Gamma_{CONST}, \Delta_A \vdash 01-04:\diamond \qquad \qquad \qquad \text{V IV B.3}$$

$$\text{VII} \quad \Gamma_B \vdash \text{x:int} \qquad \qquad \qquad \text{B.33}$$

$$\text{VIII} \quad \Gamma_B \vdash 10:((\bullet, \ddagger), \emptyset) \qquad \qquad \qquad \text{VII B.26}$$

$$\text{IX} \quad \Gamma_B \vdash 09-11:(LI, \ddagger), \emptyset \qquad \qquad \qquad \text{VIII B.11}$$

$$\text{X} \quad \Gamma_B \vdash 08-12:\emptyset \rightarrow ((LI, \ddagger), \emptyset) \qquad \qquad \qquad \text{IX B.6}$$

$$\text{XI} \quad \Gamma_B \setminus w_B \vdash 07-12:T_B \qquad \qquad \qquad \text{VII X B.4}$$

$$\text{XII} \quad \Gamma_B \setminus w_B \vdash B : T_B \qquad \qquad \qquad \text{B.33}$$

$$\text{XIII} \quad \Gamma_{CONST}, \Delta_B \vdash 06-13:\diamond \qquad \qquad \qquad \text{XII XI B.3}$$

$$\text{XIV} \quad \Gamma_C \vdash "815":\text{int} \qquad \qquad \qquad \text{B.33}$$

$$\text{XV} \quad \Gamma_C \vdash 19:w_B \qquad \qquad \qquad \varepsilon_{act}:\emptyset \text{ XIV B.17}$$

$$\text{XVI} \quad \Gamma_C \vdash p:T_B \qquad \qquad \qquad \text{B.33}$$

$$\text{XVII} \quad \Gamma_C \vdash 18-20:((LI, \ddagger), \emptyset) \qquad \qquad \qquad \text{XVI XV } w_B < w_B \text{ B.15}$$

$$\text{XVIII} \quad \Gamma_C \vdash 17-21:\emptyset \rightarrow ((LI, \ddagger), \emptyset) \qquad \qquad \qquad \text{XVII B.6}$$

$$\text{XIX} \quad \Gamma_C \setminus w_C \vdash 16-21:w_C \rightarrow ((LI, \ddagger), \emptyset) \qquad \qquad \qquad \text{XVI XVIII B.4}$$

$$\text{XX} \quad \Gamma_C \setminus w_C \vdash C:w_C \rightarrow ((LI, \ddagger), \emptyset) \qquad \qquad \qquad \text{B.33}$$

$$\text{XXI} \quad \Gamma_{CONST}, \Delta_C \vdash 15-22:\diamond \qquad \qquad \qquad \text{XX XIX B.3}$$

XXII	$\Gamma_D \vdash A:T_A$	B.33
XXIII	$\Gamma_D \vdash 30:\{(p \mapsto T_A)\}$	$\varepsilon_{act}:\emptyset$ XXII B.17
XXIV	$\Gamma_D \vdash C:w_C \rightarrow ((LI,\ddagger),\emptyset)$	B.33
XXV	$\vdash w_B < w_A$	array/record subtyping
XXVI	$\vdash ((\circ,\ddagger),\emptyset) < ((LI,\ddagger),\emptyset)$	layout subtyping
XXVII	$\vdash T_A < T_B$	XXV XXVI page subtyping
XXVIII	$\vdash \{p \mapsto T_A\} < w_C$	XXVII record subtyping
XXIX	$\Gamma_D \vdash 29-31:((LI,\ddagger),\emptyset)$	XXIV XXIII XXVIII B.15
XXX	$\Gamma_D \vdash B:T_B$	B.33
XXXI	$\Gamma_D \vdash 33:w_C$	$\varepsilon_{act}:\emptyset$ XXX B.17
XXXII	$\Gamma_D \vdash 31-32:((LI,\ddagger),\emptyset)$	XXIV XXXI $w_c < w_c$ B.15
XXXIII	$\Gamma_D \vdash (LI,\ddagger) \sqcup (LI,\ddagger) = (LI,\ddagger) \wedge \emptyset \odot \emptyset = \emptyset$	
XXXIV	$\Gamma_D \vdash 29-34:((LI,\ddagger),\emptyset)$	XXIX XXXII XXXIII B.9
XXXV	$\Gamma_D \vdash 28-35:((\bullet,\ddagger),\emptyset)$	XXXIV B.10
XXXVI	$\Gamma_D \vdash 25-37:\emptyset \rightarrow \square$	XXXV B.5
XXXVII	$\Gamma_D \vdash D:\emptyset \rightarrow \square$	
XXXVIII	$\Gamma_D^{FINAL}, \Delta_D \vdash 24-38:\diamond$	XXXVII XXXVI B.3
XXXIX	$(dom \Delta_A) \cap (dom \Delta_B) = \emptyset$ $\wedge ((dom \Gamma_{CONST}) \triangleleft \Delta_B) = \emptyset = ((dom \Delta_A) \triangleleft \Gamma_{CONST})$ $\wedge ((dom \Gamma_{CONST}) \triangleleft \Delta_A) = \emptyset = ((dom \Delta_B) \triangleleft \Gamma_{CONST})$	
XXXX	$\Gamma_{CONST}, \Delta_A \cup \Delta_B \vdash 01-13:\diamond$	XXXIX VI XIII B.2
XXXXI	analog of XXXIX concerning $(\emptyset, \Delta_A \cup \Delta_B)$ and $(\emptyset, \Delta_D)$	
XXXXII	$\Gamma_{CONST}, \Delta_A \cup \Delta_B \cup \Delta_C \vdash 01-22:\diamond$	XXXXI XXXX XI B.2
XXXXIII	$(dom (\Delta_A \cup \Delta_B \cup \Delta_C)) \cap (dom \Delta_D) = \emptyset$ $\wedge (dom \Gamma_D^{FINAL}) \triangleleft (\Delta_A \cup \Delta_B \cup \Delta_C) = (dom (\Delta_A \cup \Delta_B \cup \Delta_C)) \triangleleft \Gamma_D^{FINAL}$ $\wedge (dom \Gamma_{CONST}) \triangleleft \Delta_D = (dom \Delta_D) \triangleleft \Gamma_{CONST}$	
XXXXIV	$\Gamma_{CONST}, \Delta_A \cup \Delta_B \cup \Delta_C \cup \Delta_D \vdash 01-38:\diamond$	XXXXIII XXXXII XXXVIII B.2
XXXXV	$\Gamma_{CONST}, \Delta_A \cup \Delta_B \cup \Delta_C \cup \Delta_D \vdash 01-38:\checkmark$	XXXXIV ( $\Gamma_{CONST} \in \mathbb{R}$ ) B.1

## B.8 Example Type Derivation II

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**Listing B.2**

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```
01 <form callee="target">
02   <code>
03     if cond then
04       while cond do
05         </code>
06         <object param="x">
07           <input param="name" type="String">
08             <object param="next">
09               <input param="name" type="String">
10                 </object>
11               </object>
12             <code>
13             ;
14           </code>
15           <object param="x">
16             <input param="name" type="String">
17               <object param="address">
18                 <input param="street" type="String">
19                 <input param="zip" type="int">
20                   </object>
21               </object>
22             <code>
23           else
24             </code>
25             <select param="x">
26               <option>
27                 <value> v </value>
28                 <label> l </label>
29               </option>
30             </select>
31           <code>
32         </code>
33         <submit/>
34   </form>
```

---

---

Listing B.3

---

```

01 <nsp name="target">
02   <param name="x" type="array of
03            $\mu X. \{name \mapsto \text{String},$ 
04            $address \mapsto \{street \mapsto \text{String},$ 
05            $zip \mapsto \text{int}\},$ 
06            $next \mapsto X$ 
07         }"
08   />
09   <html>
10   ...
11   </html>
12 </nsp>

```

---

$$w_{target} \equiv_{\text{DEF}} \{ x \mapsto \text{array of } \mu X. \{name \mapsto \text{String}, address \mapsto \{street \mapsto \text{String}, zip \mapsto \text{int}\}, next \mapsto X\} \}$$

$$\Gamma \equiv_{\text{DEF}} \{ cond \mapsto \text{boolean}, v \mapsto \mu X. \{name \mapsto \text{String}, address \mapsto \{street \mapsto \text{String}, zip \mapsto \text{int}\}, next \mapsto X\}, l \mapsto \text{String}, target \mapsto (w_{target} \rightarrow \square) \}$$

I	$\Gamma \vdash 09:((\bullet, \Downarrow), \{name \mapsto \text{String}\})$	B.22
II	$\Gamma \vdash 08-10:((\bullet, \Downarrow), \{next \mapsto \{name \mapsto \text{String}\}\})$	I B.19
III	$\Gamma \vdash 07:((\bullet, \Downarrow), \{name \mapsto \text{String}\})$	B.22
IV	$\Gamma \vdash 07-10:((\bullet, \Downarrow), \{name \mapsto \text{String}, next \mapsto \{name \mapsto \text{String}\}\})$	I III B.9
V	$\Gamma \vdash 06-11:((\bullet, \Downarrow), \{x \mapsto \{name \mapsto \text{String}, next \mapsto \{name \mapsto \text{String}\}\}\})$	IV B.19
VI	$\Gamma \vdash 05-12:((\bullet, \Downarrow), \{x \mapsto \{name \mapsto \text{String}, next \mapsto \{name \mapsto \text{String}\}\}\})$	V B.28
VII	$\Gamma \vdash cond : \text{boolean}$	B.33
VIII	$\Gamma \vdash 04-12:((\bullet, \Downarrow), \{x \mapsto \text{array of } \{name \mapsto \text{String}, next \mapsto \text{String}, next \mapsto \{name \mapsto \text{String}\}\}\})$	VII VI B.31
IX	$\Gamma \vdash 19:((\bullet, \Downarrow), \{zip \mapsto \text{int}\})$	B.22
X	$\Gamma \vdash 18:((\bullet, \Downarrow), \{street \mapsto \text{String}\})$	B.22
XI	$\Gamma \vdash 18-19:((\bullet, \Downarrow), \{street \mapsto \text{String}, zip \mapsto \text{int}\})$	IX X B.9
XII	$\Gamma \vdash 17-20:((\bullet, \Downarrow), \{address \mapsto \{street \mapsto \text{String}, zip \mapsto \text{int}\}\})$	XI B.19
XIII	$\Gamma \vdash 16:((\bullet, \Downarrow), \{name \mapsto \text{String}\})$	B.22
XIV	$\Gamma \vdash 16-20:((\bullet, \Downarrow), \{name \mapsto \text{String}, address \mapsto \{street \mapsto \text{String}, zip \mapsto \text{int}\}\})$	XIII XII B.9
XV	$\Gamma \vdash 15-21:((\bullet, \Downarrow), \{x \mapsto \{name \mapsto \text{String}, address \mapsto \{street \mapsto \text{String}, zip \mapsto \text{int}\}\}\})$	XIV B.19

XVI	$\Gamma \vdash 14\text{-}22:((\bullet, \Downarrow), \{x \mapsto \{name \mapsto \text{String}, address \mapsto \{street \mapsto \text{String}, zip \mapsto \text{int}\}\}\})$	XV B.28
XVII	$\Gamma \vdash 04\text{-}22:((\bullet, \Downarrow), \{x \mapsto \text{array of } \{name \mapsto \text{String}, address \mapsto \{street \mapsto \text{String}, zip \mapsto \text{int}\}, next \mapsto \{name \mapsto \text{String}\}\}\})$	VIII XVI B.29
XVIII	$\Gamma \vdash v:\mu X.\{name \mapsto \text{String}, address \mapsto \{street \mapsto \text{String}, zip \mapsto \text{int}\}, next \mapsto X\}$	B.33
XIX	$\Gamma \vdash l:\text{String}$	B.33
XX	$\Gamma \vdash 26\text{-}29:((OP, \Downarrow), \{x \mapsto \text{array of } \mu X.\{name \mapsto \text{String}, address \mapsto \{street \mapsto \text{String}, zip \mapsto \text{int}\}, next \mapsto X\}\})$	XVIII XIX B.25
XXI	$\Gamma \vdash 25\text{-}30:((\bullet, \Downarrow), w_{target})$	XX B.24
XXII	$\Gamma \vdash 24\text{-}31:((\bullet, \Downarrow), w_{target})$	XXI B.28
XXIII	$\Gamma \vdash 03\text{-}31:((\bullet, \Downarrow), w_{target})$	XVII XXII B.30
XXIV	$\Gamma \vdash 02\text{-}32:((\bullet, \Downarrow), w_{target})$	XVIII B.27
XXV	$\Gamma \vdash 33:((\bullet, \Downarrow), \emptyset)$	B.21
XXVI	$\Gamma \vdash 02\text{-}33:((\bullet, \Downarrow), w_{target})$	XXIV XXV B.9
XXVII	$\Gamma \vdash target : w_{target} \rightarrow \square$	B.33
XXVIII	$\Gamma \vdash 01\text{-}34:((\bullet, \Uparrow), \emptyset)$	XXVII XXVI $\vdash w_{target} < w_{target}$ B.18