

# The Output Effects of Commodity Price Volatility: Evidence from Exporting Countries

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# The Output Effects of Commodity Price Volatility: Evidence from Exporting Countries\*

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## Abstract

Empirical evidence indicates that high oil price volatility has a dampening effect on output in countries that import commodities. Many countries, however, gain important revenues from commodity exports. This paper investigates the output effects of commodity price volatility in commodity exporting countries accounting for both oil and non-oil commodities. To that aim, we construct country specific commodity price indices for a sample of oil and non-oil commodity exporters. We find a significant negative impact of price volatility on real output for oil exporters. Our results for exporters of other commodities, however, suggest that the volatility effect is a peculiar feature of oil and not generalizable to a broad basket of commodities.

JEL-Classification: C32, O13, Q43

Keywords: commodity price uncertainty, commodity exporters, VAR-MGARCH-in-mean.

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# 1 Introduction

In the first decade of the new century commodity price volatility reached historically high levels. Large price fluctuations gained attention by both policymakers and policy advisors worldwide. The G20 summit in 2011, for instance, identified commodity price volatility as a concerning issue arguing that increased volatility creates uncertainty over future price levels which complicates investment and hampers economic growth.<sup>1</sup> This notion is in line with the theoretical literature on investment under uncertainty (see Bernanke, 1983, Pindyck, 1991, or, Dixit and Pindyck, 1994) and empirical contributions that find a negative effect of uncertainty about future oil prices on real output in several commodity importing G7 countries (Elder and Serletis, 2010, 2011, Bredin et al., 2011).<sup>2</sup>

A negative volatility effect, however, should be of particular importance for the large group of countries that rely on primary commodity exports as an essential source of income. Trade data from the United Nations Conference on Trade and Development (UNCTAD) shows that out of 216 countries, more than two-thirds have a share of primary commodities in total exports that exceeds 30 %. In this regard, oil is not the only commodity of interest. Of the countries with such a large share in exports, only 20 % export mainly oil or other fuels while 80 % generate export revenues mainly from primary commodities like minerals, metals, and agricultural products.

Against this background, the aim of our paper is twofold. First, we estimate the output effects of commodity price volatility for countries that export, not import, commodities. Second, we investigate whether the output effects of commodity price volatility differ for oil and non-oil commodities. To that aim, our sample consists of countries where commodities account for an important share of exports. We use international trade data to construct country specific commodity export price indices based on a basket of 48 different commodities ranging from petroleum products, metals, and agricultural raw materials to food. In doing so, we assure that the distinct commodity export structures of the sample countries are taken into account. In particular, constructing country specific indices allows us to identify the group of countries where petroleum products constitute an important share of commodity exports.

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<sup>1</sup>For example, Nicolas Sarkozy, then President of the French Republic and representing the French G20 presidency, addressed the G20 agriculture ministers' meeting during his opening speech: "Volatility, let us be absolutely clear about this, is a scourge. Volatility is a scourge for small farmers and for consumers, as well as for the stability of States; volatility is a threat because it endangers agricultural productivity for years to come: what farmer can commit himself to major investment when he is at risk of losing a third of his income the following year? What businessman would risk investing in such an unstable market?"

<sup>2</sup>Empirical evidence for an effect of oil price uncertainty on the micro level is found by Kellogg (2014). Using data on oil drilling in Texas, he shows that firms adjust their drilling activity in response to changes in price volatility.

Our work is linked to the considerable number of studies that have empirically analyzed the impact of general economic uncertainty on economic aggregates (see, for instance, Ramey and Ramey, 1995, Bloom, 2009, Gourio et al., 2013, or Carrière-Swallow and Céspedes, 2013). It relates more closely to the less researched field on the effect of commodity price uncertainty. One group of studies analyzes the relation between commodity price volatility and output growth over long time periods using homogeneous panel techniques (Blattman et al., 2007, Arezki and Gylfason, 2011, Cavalcanti et al., 2014).<sup>3</sup> We supplement these studies by analyzing the effect of commodity export price volatility for individual countries at the business cycle frequency. In particular, we follow a seminal contribution by Elder and Serletis (2010) who use a structural VAR accommodated by GARCH-in-mean errors to analyze the impact of oil price uncertainty on real economic activity in the US. They find that uncertainty about the future oil price has a significant negative effect on real economic activity. Uncertainty is thereby measured as the conditional standard deviation of the forecast error of the oil price change. In a subsequent paper, Elder and Serletis (2011) detect the same negative effect also with monthly data on industrial production and manufacturing. Similar work by Elder and Serletis (2009), Bredin et al. (2011) and Rahman and Serletis (2012) finds evidence for this volatility effect in four of the G7 countries (UK, US, France, and Canada) while Aye et al. (2014) detect it for South Africa. Jo (2014) shows that the oil price uncertainty effect is not limited to explicit GARCH modeling, but also appears in a VAR model with stochastic volatility in mean. Moreover, she finds that higher price uncertainty is related to a reduction of world industrial production.<sup>4</sup>

Our main results can be summarized as follows. Confirming earlier evidence for oil importers, we find that price volatility has a negative effect on real output for the oil exporting countries in our sample. Impulse response analysis shows that the increase in volatility accompanying a price shock has dampening effects on the real economy over several months. However, for the other countries in our sample that mainly rely on non-energy commodity exports like minerals, metals, and agricultural products, we find that commodity price volatility has no significant effect on real output.

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<sup>3</sup>Blattman et al. (2007) show that higher terms-of-trade volatility, attributed to commodity prices, was detrimental for growth in then less industrialized countries between 1870 and 1939. Cavalcanti et al. (2014) use a panel with annual data for 1970-2007 and find that commodity terms-of-trade volatility offsets the positive impact of commodity booms in countries that export primary commodities. Arezki and Gylfason (2011) employ a similar panel for 1970-2007, but consider the growth of non-resource GDP instead. They find that price volatility leads to a significant increase in non-resource GDP growth in democracies, but to no significant increase in autocracies.

<sup>4</sup>The research on oil price uncertainty is related to a large empirical literature that models the role of oil prices in the real economy (see, for instance, Hamilton, 2009, Kilian, 2009, and, Kilian and Murphy, 2014).

The remainder of the paper is structured as follows. In Section 2, we describe the countries under consideration, the construction of commodity price indices, and the VAR-GARCH-in-mean model. In Section 3, we present the empirical results on the output effects of commodity price volatility. Section 4 contains a complementary impulse response analysis. Section 5 concludes.

## 2 Price Volatility and Commodity Exporting Countries: Data

In this section, we discuss the selection of sample countries and how we construct the indices and transform the data. Moreover, we briefly outline the employed VAR-GARCH-in-mean model.

### 2.1 Commodity Exporting Countries

Our analysis focuses on countries whose exports consist to a large extent of primary commodities. The group of possible candidates mainly encompasses developing countries in Africa, Asia and Latin America. Unfortunately, output data on a business cycle frequency are not available for most of these countries. For this reason, we restrict our analysis to the following countries: Australia, Brazil, Canada, Chile, Indonesia, Mexico, New Zealand, Norway, and South Africa.<sup>5</sup>

This choice is based on a threshold which requires commodities to account for at least 30 % of total exports in 2008. Using the threshold ensures that the countries in our sample are highly exposed to swings in commodity prices. More importantly, their export share is considerably higher than in industrialized countries considered to be major commodity importers.

Table 1: Share of Commodities in Exports

	share of comm. in total exp.	share of petrol. in comm. exp.		share of comm. in total exp.	share of petrol. in comm. exp.
Australia	0.67	0.16	Mexico	0.21	0.82
Brazil	0.44	0.21	New Zealand	0.34	0.20
Canada	0.39	0.65	Norway	0.77	0.88
Chile	0.71	0.03	South Africa	0.39	0.06
Indonesia	0.56	0.38			

The table shows the value share of the 48 commodities included in the commodity price indices in total exports and the value share of petroleum products in the 48 used commodities. Numbers are author's own calculations based on UNCTAD trade data for 2008.

<sup>5</sup>Notable omissions from the sample include countries in South America like Argentina, Colombia, Peru, or Paraguay, where monthly data on industrial production are to some extent available going back to the 1980s. However, both the noisy and crisis driven industrial production series as well as the recurring currency crisis prevent us from obtaining meaningful results for these countries.

Table 1 shows the value share of commodities in total exports for our sample countries calculated with UNCTAD trade data. The only country for which exports lie below the threshold is Mexico. Note, however, that the share of commodity exports in official trade data for Mexico is known to be downward biased due to the ‘extended workbench’ function of the so called ‘Maquilla Sector’ (see Jiménez and Tromben, 2006). This means that the share of commodities in exports is larger than the official UNCTAD data suggest. The importance of commodities can also be inferred from the share of commodity exports in GDP (Table 4 in the appendix) which exceeds 10 % for almost all our sample countries.

Our sample of countries not only allows us to investigate whether the results for uncertainty about future prices can be generalized to commodity exporters. It also allows us to test whether the results of the literature are a peculiar property of uncertainty about oil prices or if they translate to a broad basket of commodities. For this purpose, we henceforth split our sample of countries into two groups: oil exporters and non-oil exporters.

The UNCTAD trade data in Table 1 show that the former classification applies to Canada, Norway, and Mexico whose commodity exports consists to more than two thirds of oil (petroleum products). The only other country with a share of more than one-fifth of oil in commodity exports is Indonesia. Although it terminated its OPEC membership in 2008 and became a net crude oil importer, the country has been a net petroleum exporter for most of the sample period. Therefore, we consider it, along with Canada, Norway, and Mexico, as an oil exporter in our analysis.

For the other countries in our sample, petroleum products play only a minor role. Their major share of commodity exports consists of minerals, metals, and agricultural products. Hence we will consider this group of countries, Australia, Brazil, Chile, New Zealand, and South Africa, as non-oil commodity exporters.

## **2.2 Commodity Export Price and Real Output Measures**

For our empirical analysis, we construct country specific commodity price indices. This takes into account the country specific commodity export structures, which differ substantially between our sample countries. We apply the approach of UNCTAD (2012) which includes a broad range of commodities and relies on the UNCTAD trade database to ensure data consistency.

Price indices are computed as geometric Laspeyres indices with a fixed base period  $b$  as

introduced in the commodity literature by Deaton and Miller (1995):

$$I_{i,t}^b = \prod_j P_{j,t}^{W_{j,i}^b}. \quad (1)$$

$I_{i,t}^b$  is the value of the commodity index in country  $i$  at time  $t$ ,  $P_{j,t}$  is the international dollar price of commodity  $j$  at time  $t$  and the weight  $W_{j,i}^b$  is the value share of this commodity  $j$  in country  $i$ 's commodity export basket in a base period  $b$ . The baskets are based on monthly prices of 48 commodities which cover minerals, metals, agricultural raw materials, food, petroleum products, and other energy commodities. Together, these commodities account for the major share of the commodities traded worldwide over the past decades. Trade data is taken from the UNCTAD database while price data are based on the IMF database and UNCTAD computations.<sup>6</sup> The constructed nominal indices are displayed in Figure 1 and reveal two interesting facts. Firstly, there are pronounced differences between countries despite a general co-movement. Secondly, the co-movement is generated by rather stable prices until the onset of the commodity boom in the last decade.

For investment decisions and real output, real and not nominal prices are crucial. Therefore, we convert the nominal indices to real terms for the VAR-GARCH-in-mean estimations. Doing this also takes the volatility in the foreign exchange rate and in consumer prices into account.<sup>7</sup>

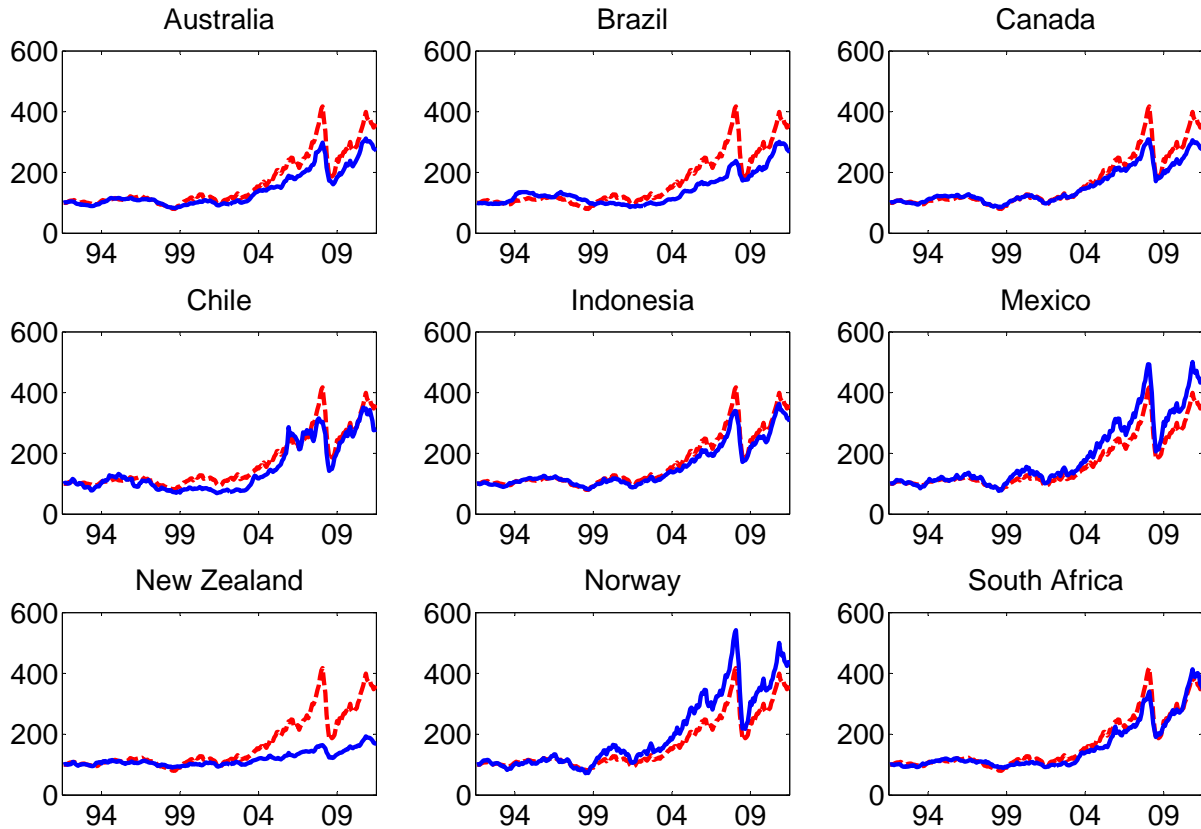
As a proxy for real output we use seasonally adjusted real indices of industrial production. This has the advantage that data is available on a monthly frequency which ensures a sufficient number of observations for a consistent estimation. More importantly, the commodity price indices are also available on a monthly frequency. Using industrial production allows us to make use of their full information content. For Australia and New Zealand, no monthly index of

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<sup>6</sup>We computed the country specific commodity weights based on trade volume matrices for imports and exports publicly available at the UNCTAD database. We follow UNCTAD (2012) and take 1995, which is in the midst of our sample, as the base year for the export weights. The indices, however, are robust to changing the base period to 2000 or 2008. Moreover, the indices with geometric weights are highly correlated with indices constructed with linear weights. A detailed description of the included commodities can be found in appendix A. We are grateful that Jörg Mayer at UNCTAD provided us with the commodity price series of UNCTAD (2012). Unfortunately, some of the prices for the included commodities rely on UNCTAD calculations and are not available at public databases so that our sample ends in 2011.

<sup>7</sup>To convert the nominal US dollar indices to real terms, they are in a first step multiplied with the respective foreign exchange rate. The resulting nominal local currency indices are then deflated by the country specific consumer price index (CPI) to have a real measure of commodity price developments. Another possibility to control for foreign exchange rates and local consumer prices would be to include them as endogenous variables in the estimation. However, including additional variables in the VAR-GARCH-in-mean estimation considerably enlarges the parameter space. For this highly nonlinear model, the maximum likelihood estimation procedure faces difficulties optimizing over an extensive parameter space. We hence stick to a parsimonious bivariate model in real terms.

Figure 1: Nominal Commodity Export Price Indices (with IMF index as benchmark)



Figures show the nominal commodity export prices indices for the individual countries (blue solid lines). As a benchmark and for comparison, they are plotted along the general IMF commodity index (red dashed lines). Base year for the indices is 1995.

industrial production is available. In this case, we use quarterly data on real GDP (Australia) and manufacturing production (New Zealand) as a measure of real output and take quarterly averages of the commodity price index.<sup>8</sup> Data on industrial production, foreign exchange rates (both spot market and PPP adjusted), and consumer prices are taken from the OECD database and the IFS statistics of the IMF.

Our econometric approach strongly relies on stationarity of the data for a consistent estimation. Therefore, we take logarithmic differences of both the real commodity export price indices and industrial production to ensure stationarity, i.e. we analyze the underlying relationship in growth rates in accordance with the literature on oil price uncertainty (Elder and Serletis, 2010, 2011, Rahman and Serletis, 2011, Bredin et al., 2011).<sup>9</sup>

The earliest starting date with monthly data is January 1980. Prior to 1980, commodities

<sup>8</sup>Quarterly GDP for New Zealand is available only since 1987. Therefore, we use the manufacturing series and not real GDP as otherwise the sample would consist of far less than 100 observations.

<sup>9</sup>Results of unit root tests for the individual series in (log-)levels are available upon request. They predominantly point towards series being non-stationary both for industrial production and real commodity price indices.



exhibited long periods of rather constant prices with rare but rapid adjustments. By choosing this starting date we avoid modeling a possible break in commodity markets after which prices were more flexible. For Australia and New Zealand, less data are available due to the quarterly frequency. Here, we report results starting in 1974 (Australia) and 1977 (New Zealand), however, results prove to be robust to the selection of a later starting date. Our sample ends in December 2011. As a robustness check, we also run several estimations with a shortened sample up to December 2007. In doing so we intend to ensure that our results are not solely driven by the 2008/09 economic crisis. This is because we fear that the simultaneous increase in volatility and decline in industrial production, caused by the global turmoil on financial markets, might spuriously induce a correlation that is not present in tranquil times.

### 2.3 The VAR-MGARCH-in-mean model

The empirical model for our main analysis is a (bivariate) structural vector autoregression (SVAR) which is augmented by conditional heteroskedasticity in the parametric form of multivariate GARCH-in-mean as developed in Elder (2004).<sup>10</sup> In its structural form, the model can be written as follows:

$$By_t = C + A_1y_{t-1} + A_2y_{t-2} + \dots + A_p y_{t-p} + \Lambda(L)h_t^{1/2} + \varepsilon_t, \quad (2)$$

$$h_t = \text{diag}(H_t) = k + \sum_{i=1}^q F_i \text{diag}(\varepsilon_{t-i} \varepsilon'_{t-i}) + \sum_{j=1}^r G_j h_{t-j}, \quad (3)$$

with  $y_t$  being an  $n$ -dimensional vector that contains the realization of the endogenous variables in period  $t$ . Conditional on the information set  $\Omega_{t-1}$ , that includes all variables dated  $t-1$  and earlier, the structural innovations  $\varepsilon_t$  are assumed to be independently normally distributed with mean zero and conditional covariance matrix  $H_t$ ,  $\varepsilon_t | \Omega_{t-1} \sim N(0, H_t)$ .  $H_t$  is modeled as a multivariate GARCH process as given in Equation (3), where  $\text{diag}$  is the operator that extracts the diagonal from a square matrix.

We follow Elder (2004) and Elder and Serletis (2010, 2011) and impose the subsequent assumptions. First, as commonly done, we assume that the structural innovations are contemporaneously (and conditionally) uncorrelated so that  $H_t$  is a diagonal matrix. Second, we assume that the conditional variance of  $y_{i,t}$  depends only on its own past squared errors and its own past conditional variances, so that parameter matrices  $F_i$  and  $G_j$  are also diagonal.<sup>11</sup> Third, we choose

<sup>10</sup>VAR models with GARCH-in-mean errors were first introduced by Engle and Kroner (1995).

<sup>11</sup>The assumption that the innovations are conditionally uncorrelated is stronger than necessary in a dynamic setting, however, it considerably simplifies the multivariate variance functions and reduced the large parameter

a parsimonious lag length of  $q = r = 1$  for the MGARCH process.

Volatility of commodity prices is measured in this model by the conditional standard deviation  $h_t^{1/2}$  of the respective structural innovation. This can also be interpreted as the standard deviation of the one-step-ahead (structural) forecast error making  $h_t^{1/2}$  a measure of dispersion in the forecast and, therefore, a proxy of uncertainty about future commodity price developments.

In the VAR-GARCH-in-mean specification, the variables contained in  $y_t$  are affected by conditional volatility if the elements in  $\Lambda(L)$  differ from zero. Several lags of  $h_t^{1/2}$  could be included in the mean equation. It has to be kept in mind, however, that  $h_t$  itself is already correlated with its past realizations. Therefore, we decide to follow Elder and Serletis (2010, 2011) and include only the contemporaneous conditional standard deviation. This has the advantage that testing the effect of commodity price volatility on real output comes down to the statistical significance of a single element.

To identify the structural system, a sufficient number of identification restrictions has to be imposed on matrix B. We use zero restrictions as in a homoskedastic VAR and allow industrial production to react instantaneously to innovations in real commodity prices but not vice versa.<sup>12</sup> Hence, we assume that shocks to industrial production affect international commodity prices only with a lag. The reasoning is that the commodity exporting countries in our dataset are too small for their domestic shocks to affect world market prices of commodities right away. This identification strategy is in line with commonly applied Cholesky orderings in SVAR models for our sample countries, where the commodity price index is usually ordered first (see, for instance, Berkelmans, 2005, for Australia, or Medina, 2010, for Latin America). Furthermore, it is in accordance with the SVAR-GARCH-in-mean specifications for oil prices by Elder and Serletis (2010) or Bredin et al. (2011).<sup>13</sup> To further analyze the dynamic properties of our estimated models we use impulse response functions (IRFs) for the SVAR-GARCH-in-mean as derived by Elder (2003). This is necessary since standard IRFs do not apply to this nonlinear model. A description of the IRFs can be found in the appendix.

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space of this highly nonlinear model. The same holds for the second assumption.

<sup>12</sup>Different to a homoskedastic VAR, B cannot be recovered in a second step by a Cholesky decomposition or maximum likelihood estimation (Elder, 2004). The system of equations is, therefore, estimated consistently in one step by applying a full information maximum likelihood (FIML) approach.

<sup>13</sup>Other researchers dealing with US data, like Elder and Serletis (2011), assume that oil prices react instantaneously to output shocks as they can adjust rapidly to new information. This, however, is not necessarily the case in our work as countries are too small to have an immediate effect on international prices and not all commodities in our indices are traded on highly liquid markets.

### 3 Is Commodity Export Price Volatility Harmful?

In this section we present the estimated relation between commodity price uncertainty and real output. We look at oil exporting countries first, then turn to the non-oil exporters and, lastly, evaluate the robustness of our results. Before looking at the point estimates, however, it is worth noting that we find significant GARCH effects in the commodity export price series for all sample countries and, predominantly, also in the series on industrial production. These significant GARCH effects support the VAR-MGARCH specification. Further evidence in favor of the VAR-MGARCH-in-mean is given by the Schwartz information criterion. For almost all countries the criterion points towards a better fit of the model compared to a homoskedastic VAR.<sup>14</sup>

Table 2 and 3 report the point estimates for the oil and non-oil exporting countries, respectively. The parameter capturing the effect of commodity price volatility on real output is  $\Lambda_{(1,2)}$ , the upper off-diagonal element of the volatility spillover matrix  $\Lambda$ .<sup>15</sup> Lag lengths for our baseline estimations are selected by the Akaike information criterion (AIC) which yields residuals free from autocorrelation. As a robustness specification, estimations based on the Schwartz criterion (SIC) confirming our main results can be found in Table 6 in the appendix.

#### 3.1 Oil Exporting Countries

The VAR-GARCH-in-mean estimations show an adverse effect of commodity price volatility on real output for the oil exporting countries (see Table 2). The point estimates for Canada and Norway clearly indicate a negative impact of commodity export price volatility on real output. This holds for the complete sample and for a sample excluding the crisis period since 2008. Results for Indonesia display a similar negative impact. Hereby, the baseline estimation starts with the earliest available data in 1986. A further estimation controls for a possible bias due to the Asian crisis, which heavily affected the country, by letting the sample start in 1999. For Mexico, results from the main specification show a negative effect with significance

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<sup>14</sup>The estimated MGARCH equations can be found in Table 5 in the appendix. The table also contains the Schwartz information criterion for our baseline VAR-MGARCH-in-mean and for the corresponding homoskedastic VAR model.

<sup>15</sup>In the reported estimations, we restricted the elements of  $\Lambda$  measuring spillovers from industrial production volatility to zero. This is empirically supported by the Schwartz information criterion and individual significance tests and in line with economic reasoning as volatility in the industrial production series should not affect world market commodity prices. The parameter capturing the spillover of export price volatility on the commodity price itself is predominantly found to be insignificant and not reported.

given at the 15% level. The robustness analysis, moreover, yields strong evidence in favor of a significant negative volatility impact. The baseline estimations for Mexico, nevertheless, have the shortcoming that the sample includes various crisis episodes. Additional estimations which exclude the "Tequila-Crisis" 1995 yield negative but insignificant estimates. However, they rely on far less observations than the baseline and could still be affected by later crisis episodes.

Table 2: Estimates of Commodity Price Volatility Coefficient: Oil Exporters

VAR-Equation: $ip_t = c + \sum_{i=1}^p a_{1,t-i} ip_{t-i} + \sum_{i=1}^p a_{2,t-i} com_{t-i} + \Lambda_{(1,2)} h(com)_t + \varepsilon_t$									
	Sample	Lags	Obs	$\Lambda_{(1,2)}$		Sample	Lags	Obs	$\Lambda_{(1,2)}$
<b>Canada</b>					<b>Indonesia</b>				
<i>Baseline</i>	80-11	3	377	<b>-0.17**</b> (0.08)	<i>Baseline</i>	86-11	2	308	<b>-0.08**</b> (0.03)
<i>Fin. Crisis excluded</i>	80-07	3	329	<b>-0.35**</b> (0.19)	<i>Asian Crisis excluded</i>	99-11	1	155	<b>-0.25**</b> (0.11)
<b>Mexico</b>					<b>Norway</b>				
<i>Baseline</i>	80-11	2	381	-0.05 (0.03)	<i>Baseline</i>	80-11	6	377	<b>-0.37**</b> (0.10)
<i>Tequila Crisis excluded</i>	96-11	2	190	-0.10 (0.08)	<i>Fin. Crisis excluded</i>	80-07	6	329	<b>-0.42**</b> (0.10)

Table shows the estimated parameter measuring the direct impact of conditional commodity price volatility on output. Lag length is based on the Akaike information criterion. Values in parentheses are asymptotic standard errors based on inverse of the Hessian.

\* - significance on 10% level, \*\* - significance on 5% level.

Given the point estimates of  $\Lambda_{(1,2)}$  some initial conclusions regarding the economic significance of the volatility effect can be drawn. As an example, we do 'back-of-the-envelope' calculation for Canada and Norway. An average change in commodity price uncertainty is associated with a drop in the monthly growth rate of industrial production by about 15 basis points in Canada and by about 34 basis points in Norway.<sup>16</sup> These calculations underline the impression that commodity price volatility matters for real economic activity in these countries. It is necessary, however, to treat these 'back-of-the-envelope' calculation with caution. Firstly, they ignore dynamic interactions between the variables. Secondly, they might ignore possible relevant reactions in other variables as they are based on a bivariate system.

<sup>16</sup>We take the standard deviation of the estimated conditional volatility series to be an average change in commodity price uncertainty.

### 3.2 Non-Oil Exporting Countries

For the other countries that export mainly minerals, metals, and agricultural commodities, coefficients are predominantly found to be insignificant, although by and large they have the expected negative sign (see Table 3). Significance in the estimations for Australia is driven by the 2008 economic crisis as it vanishes in the sample which excludes this episode. Estimations for Chile, New Zealand, and South Africa, do not display any significant point estimates at all.<sup>17</sup> The same holds true for Brazil where we take possible break points into account. We start baseline estimations for Brazil in 1995 due to the visible break point in the real price index in 1994, connected to foreign exchange and inflation turmoil as well as monetary alignment. A different sample beginning in 2003 tries to account for the Brazilian currency crisis 98/99 and the Argentinian crisis 2001 but does not yield significant results either.

Table 3: Estimates of Commodity Price Volatility Coefficient: Non-Oil Exporters

VAR-Equation: $ip_t = c + \sum_{i=1}^p a_{1,t-i} ip_{t-i} + \sum_{i=1}^p a_{2,t-i} com_{t-i} + \Lambda_{(1,2)} h(com)_t + \varepsilon_t$									
	Sample	Lags	Obs	$\Lambda_{(1,2)}$		Sample	Lags	Obs	$\Lambda_{(1,2)}$
<b>Australia</b>					<b>Brazil</b>				
<i>Baseline</i>	74-11	4	147	<b>-0.18**</b> (0.08)	<i>Baseline</i>	95-11	5	199	-0.01 (0.06)
<i>Fin. Crisis excluded</i>	74-07	4	131	-0.24 (0.31)	<i>Argent. Crisis excluded</i>	03-11	4	104	0.24 (0.11)
<b>Chile</b>					<b>New Zealand</b>				
<i>Baseline</i>	91-11	3	248	-0.30 (0.19)	<i>Baseline</i>	77-11	2	136	-0.10 (1.14)
<i>Fin. Crisis excluded</i>	91-07	3	200	-0.11 (0.29)	<i>Fin. Crisis excluded</i>	77-07	2	120	-0.01 (0.04)
<b>South Africa</b>									
<i>Baseline</i>	90-11	3	260	-0.04 (0.10)					
<i>Fin. Crisis excluded</i>	90-07	3	212	0.11 (0.13)					

Table shows the estimated parameter measuring the direct impact of conditional commodity price volatility on output. Lag length is based on the Akaike information criterion. Values in parentheses are asymptotic standard errors based on inverse of the Hessian.

\* - significance on 10% level, \*\* - significance on 5% level.

<sup>17</sup>Estimations for Chile and South Africa start with the earliest available output data.

### 3.3 Robustness

To ensure the robustness of the results, we use different measures. Firstly, we apply an alternative approach to construct the real commodity price indices. Instead of the nominal exchange rates, we use PPP-adjusted ones to address possible excess volatility issues in spot exchange rates. As a further robustness check, we analyze the relationship between commodity price volatility and real output in a single equation autoregressive distributed lag (ADL) framework with different volatility measures that were computed beforehand (univariate GARCH, rolling 3-month and 12-month standard deviations). This ensures that general findings are not solely driven by the model or the volatility measure. Results from both robustness estimations support our main findings. A detailed description of the robustness analysis can be found in appendix B.

## 4 Dynamic Impact of Commodity Export Price Shocks

So far, we have considered the statistical significance of the parameter capturing the impact of commodity price volatility on real output. In this section, we obtain a comprehensive picture by looking at how volatility affects the dynamic response of output to a commodity price shock. For this purpose, we use the Impulse-Response-Functions (IRFs) by Elder (2003) specifically developed for the SVAR-GARCH-in-mean model. To illustrate the dynamic effects, we display IRFs for Canada and Norway, two of the oil exporting countries for which the spillover coefficient is found to be statistically significant. In Figures 2 and 3, we show the response of real output to a real commodity price shock taking the volatility effect into account (blue solid line) and the response with the in-mean parameter  $\Lambda_{(1,2)}$  restricted to zero (red dashed line). This can be understood as a counterfactual analysis of how responses would differ if the volatility effect was absent.<sup>18</sup>

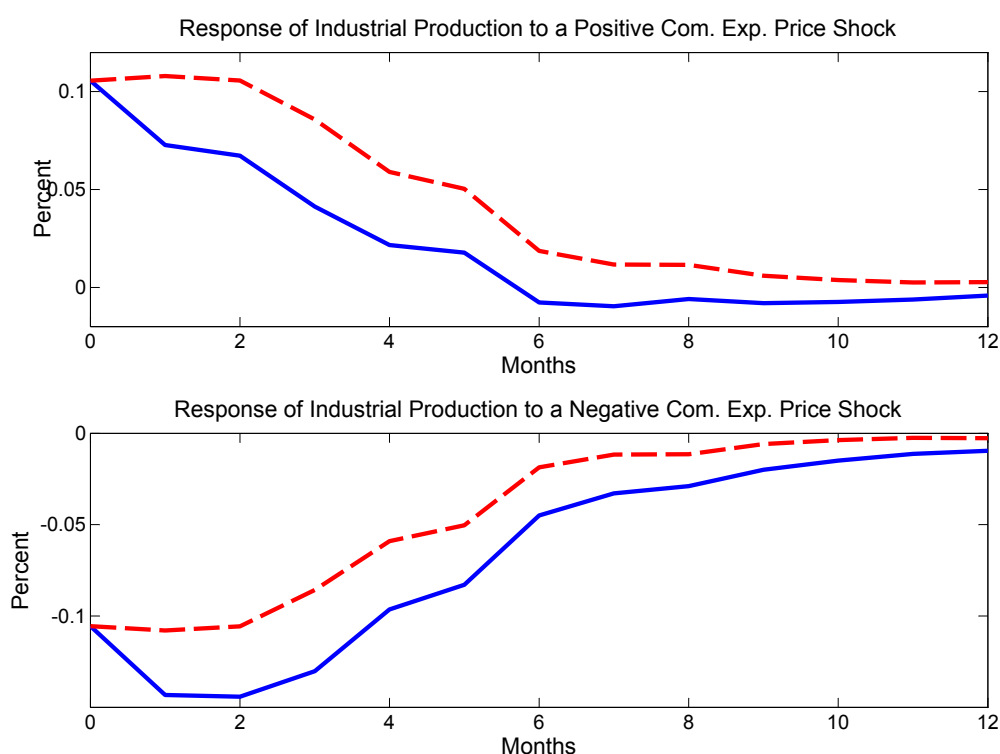
The IRFs for Canada and Norway show that the initial response of industrial production to a shock which increases commodity export prices is estimated to be positive. After the initial impulse, industrial production growth remains above its equilibrium value for several periods before the shock fades out, both in the IRFs with and without the volatility augmentation.<sup>19</sup>

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<sup>18</sup>The IRFs show responses where  $\Lambda_{(1,2)}$  has been restricted to zero after the estimation, i.e. using the same values for all the other parameters. This reflects the counterfactual nature of this exercise building on the IRFs by Elder (2003).

<sup>19</sup>Different economic mechanisms can help to explain this pattern (Solheim, 2008). Export revenues and, therewith, domestic activity initially increase with the price shock if the demand for commodities (oil) is rather inelastic. Furthermore, expenditures and investment in commodity extraction rise leading to an increase in the supply of goods and services to these industries. Lastly, domestic commodity extracting companies gain value

Figure 2: Response Functions with and without (dashed line) volatility influence - Canada



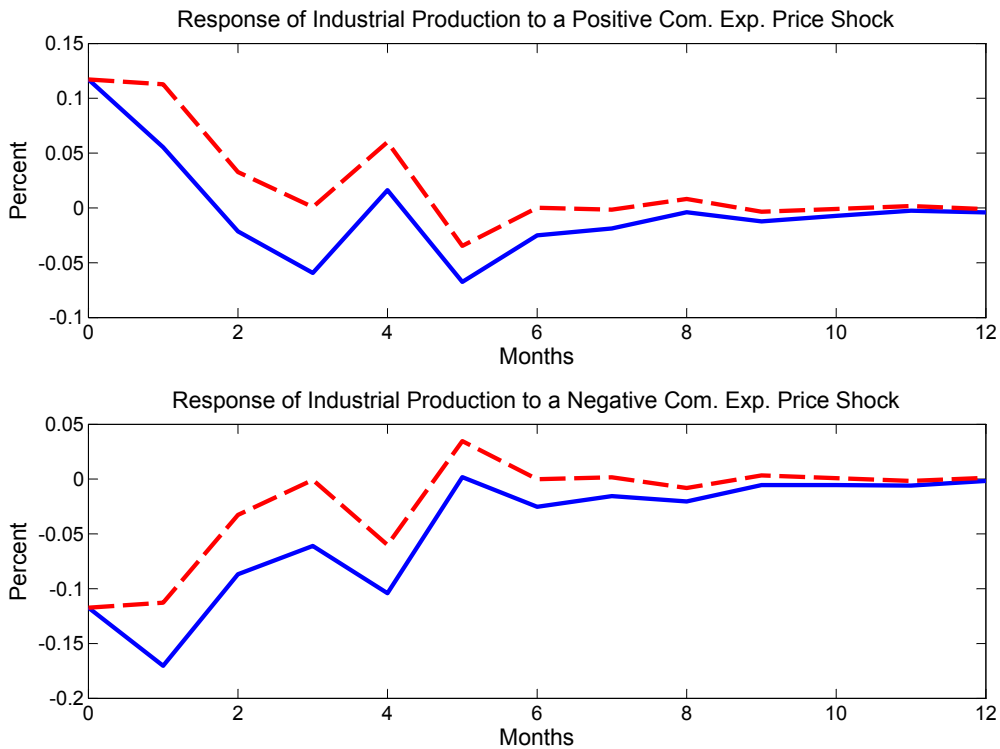
Note: The blue (solid) line displays the response of real output to a one standard deviation real commodity price impulse. It is calculated using the estimated coefficients from the SVAR-MGARCH-in-mean model based on the method developed by Elder (2003) that takes the dynamic impact of volatility on the mean ( $\Lambda$ ) into account. The red (dashed) line shows the same dynamic response with the spill-over Matrix  $\Lambda$  restricted to zero. It can be understood as a counterfactual analysis to illustrate the impact of volatility.

While displaying the same general pattern, the responses with and without the volatility effect deviate in magnitude. The positive reaction to the commodity price change is far less pronounced if the increase in uncertainty is taken into account. In fact, the response for Norway shows that industrial production growth even falls slightly below its mean between a quarter and half a year after a commodity shock. Responses stay below their restricted counterparts for a prolonged period while both revert back to the equilibrium.

Two distinct channels help to explain why the increase in uncertainty hampers the positive effect of a commodity export price shock. Firstly, volatility can dampen the expansion in investment of commodity related businesses. This is in line with the real option theory on investment under uncertainty (Bernanke, 1983, Pindyck, 1991, Dixit and Pindyck, 1994). Secondly, exports can be negatively affected through an external demand channel. For oil, Jo (2014) shows that

with rising prices resulting in a positive wealth effect. The pattern is less pronounced for Norway where responses alternate around the mean after the initial positive periods. This feature can be explained by the less persistent, but negatively autocorrelated production series.

Figure 3: Response Functions with and without (dashed line) volatility influence - Norway



Note: The blue (solid) line displays the response of real output to a one standard deviation real commodity price impulse. It is calculated using the estimated coefficients from the SVAR-MGARCH-in-mean model based on the method developed by Elder (2003) that takes the dynamic impact of volatility on the mean ( $\Lambda$ ) into account. The red (dashed) line shows the same dynamic response with the spill-over Matrix  $\Lambda$  restricted to zero. It can be understood as a counterfactual analysis to illustrate the impact of volatility.

oil price uncertainty lowers world industrial production. This can explain why an increase in commodity price uncertainty has adverse effects for oil exporting countries: it lessens export revenues and, thereby, industrial production due to an uncertainty induced fall in worldwide output and oil demand. For Canada, this effect might even be exacerbated by its close trade links to the US whose economy is strongly affected by oil price uncertainty (Elder and Serletis 2010, 2011). Norway, meanwhile, also exports other energy commodities like natural gas. Baffes (2007) shows that there is a strong link between the price developments of oil and natural gas which makes it unlikely that losses due to oil price uncertainty can be compensated by other energy commodities.

Unlike in a linear homoskedastic VAR model, the IRFs for the nonlinear VAR-MGARCH-in-mean model are not symmetric for positive and negative shocks (Elder, 2003). Beginning with Mork (1989), several authors find that responses to positive and negative oil price shocks differ. For these reasons, we also report IRFs for negative commodity price shocks. Compared to their



positive counterparts they display an inverted pattern where real output is lowered for several months. As before, the dampening effect of uncertainty leads to the volatility accounting IRFs being below the restricted ones.

Lastly, it has to be noted that we treat the counterfactual analysis with a bit of caution. Confidence bands show that the response to a commodity shock turns positive with statistical significance only for the first few months (Canada) or the initial period (Norway) if the uncertainty effect is taken into account.<sup>20</sup> Furthermore, the restricted IRFs fall into the confidence bands of the volatility accounting ones. We are hence reluctant to draw conclusions regarding the magnitude of the volatility effect from the counterfactual analysis by, for instance, measuring the gap between the two responses.

## 5 Conclusion

Commodity price volatility has been an issue on the policy agenda since the beginning of the new century. Policy makers fear a dampening effect of increased commodity price uncertainty on output. Such a negative effect of uncertainty about future oil prices has been found for the US and other oil importing industrial countries (Elder and Serletis, 2010, 2011, Bredin et al., 2011).

In this study, we build on this line of research and analyze whether price uncertainty in particular has negative output effects for commodity exporting countries. Furthermore, we investigate whether the uncertainty effect is limited to oil or also appears for a broad basket of commodities. To that aim, we construct country specific commodity price indices for a sample of oil and non-oil commodity exporting countries. We confirm a negative impact of price volatility on real output for the oil exporting countries. Impulse response analysis shows that the increase in volatility that accompanies a commodity price shock negatively affects the response of real output for a prolonged period. For the non-oil exporters, in contrast, we do not find a significant negative effect. Hence, the results do not amplify policy concerns regarding the volatility of commodities in general, but support approaches in exporting countries aimed at hedging against future oil price fluctuations, like accumulating assets in commodity funds or using derivative instruments on a macro level.

Regarding future research, it would be interesting to further evaluate the role of oil and non-oil commodity price volatility with respect to long-run growth prospects of exporting countries.

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<sup>20</sup>Responses to positive commodity price shocks with 68 % confidence bands are given in Figure 4 in the appendix.

Cavalcanti et al. (2014) find that commodity terms-of-trade volatility is harmful for long-run growth of primary commodity exporters. A possible explanation in line with our results is that oil price volatility affects not only oil exporters, but also exporters of other commodities as they have to import petroleum products. In this regard, it might prove useful to methodically combine the long-run panel studies with the SVAR-GARCH-in-mean approach by building on existing panel VAR models. On the one hand, a panel dimension is necessary to analyze a sufficiently long time period with yearly data or even 5 year averages of the data to draw conclusions about long-run effects. On the other hand, using the structural VAR-MGARCH allows for a clear identification of a commodity price shock and a dynamic impact of price uncertainty on output.

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## A Included Commodities

The 48 included commodities cover about 75 percent of world commodity exports and imports over the past decades (UNCTAD, 2012). Included in the selection are 16 food commodities (beef, other meat, fish, fishmeal, crustaceans, wheat, rice, barley, maize, meal, fruits and nuts, sugar, coffee, cocoa, tea, and spices), 13 agricultural raw materials (tobacco, hides and skins, oil seeds for soft oils, oil seeds for fixed oils, rubber, rough wood, sawn wood, cotton, jute, vegetable textile fibres, wool, fixed vegetable fats and oils, and other vegetable fats and oils), 13 minerals and metals (crude fertilizer, iron ore, copper ores, nickel ores, aluminium ores, ores of other base metals, silver, copper, nickel, aluminium, lead, zinc, and tin) as well as 6 energy commodities (coal, crude petroleum, refined petroleum, residual petroleum products, liquefied propane and butane, and natural gas). Not included are both diamonds and gold, albeit they are often categorized as commodities. On the one hand, there is no world price for diamonds, on the other hand, gold prices are strongly influenced by its role as a store of value.

## B Robustness

First indication of robustness is already given by variations in the lag length (SIC, AIC) which did not qualitatively alter the results. Another robustness check relates to the use of foreign exchange rates to convert the commodity export price indices. Cashin and McDermott (2002) find that commodity price volatility increased after the break-up of the Bretton-Woods system of fixed exchanged rates. The authors argue that instead of measuring volatility in the commodity price series one might actually measure exchange rate volatility. This concern could, in theory, also apply to our work. We address this issue by using OECD and IMF data on Purchasing Power Parity (PPP) adjusted exchange rates to build the real indices. PPP exchange rates display far less variability than nominal spot exchange rates but are only available on a much lower frequency.<sup>21</sup>

Results for the estimations with PPP adjusted real commodity price indices can be found in Table 7 (Appendix D). They remain qualitatively the same as with the nominal exchange rates. Coefficients are still estimated to be negative and significant for Canada, Norway, and Indonesia. For Mexico, the evidence for a negative effect is even stronger than in our baseline estimations. Meanwhile, significance is predominantly not found for the other countries.

To further evaluate the robustness of our results, we apply a different approach to investigate the commodity price uncertainty effect by using measures of volatility that are computed beforehand. These measures are then included as exogenous variables in models explaining industrial production. Such an approach has the caveat that it suffers from the generated regressor problem (Pagan, 1984). It can, nevertheless, provide some indication regarding the general robustness of our results.

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<sup>21</sup>Purchasing power adjusted exchange rates are available for most OECD countries on a quarterly basis while the IMF only provides PPP adjusted exchange rates on a yearly basis. We use the quarterly series and apply exponential interpolation to convert them to the monthly frequency.

We apply the following volatility measures: univariate GARCH volatility<sup>22</sup> and historical volatility given by rolling 3-month and 12-month standard deviations of the real commodity price indices.<sup>23</sup> Despite its widely use, it is not undisputed to approximate uncertainty by GARCH volatility. Applying different measures based on historical volatility is a good comparison for the GARCH results.

These measures are included in an autoregressive distributed lag (ADL) model along with log differences of the real commodity export index and of industrial production. The ADL Model takes the form:

$$y_t = \beta_0 + \sum_{i=1}^p \beta_{t-i} y_{t-i} + \sum_{i=1}^q \alpha_i x_{t-i} + \gamma z_t + \varepsilon_t, \quad (4)$$

with  $y_t$  the log growth rate of industrial production,  $x_t$  the log growth rate of the country specific commodity price index, and  $z_t$  the alternative volatility measure.

The estimated coefficients for the volatility spill-over parameter  $\gamma$  can be found in Table 8 (Appendix D). The results largely confirm the results of the VAR-MGARCH-in-mean analysis. For Canada, Mexico, and Indonesia (longer sample) all types of volatility have a significant negative effect on output while no significant effects can be detected for Australia, South Africa, New Zealand, Chile, and Brazil. Only for Norway, there is a deviation from the VAR-MGARCH-in-mean results in certain aspects. In estimations for Norway, only the GARCH volatility is significant and negative. This can be explained by the fact that one-time oil price shocks are highly reflected in the GARCH volatility while the historical volatility series are more smooth. These smoother long term fluctuations do not capture the production dampening uncertainty caused by the large oil price shocks as the GARCH process does.

## C Impulse Response Functions by Elder (2003)

Dynamic properties of VAR models are usually displayed using Impulse-Response-Functions (IRFs). Standard IRF analysis, however, cannot be conducted as the VAR-MGARCH-in-mean is a highly nonlinear model where the dynamic response to a shock depends on the size and the variance of the shock. Elder (2003) derives a closed-form solution for structural VAR models with multivariate GARCH-in-mean errors, based on the interpretation of an IRF as the revision in the conditional forecast of the variables  $y$  in period  $t+k$  given an impulse  $\varepsilon_{i,t}$ ,  $i = 1, 2$ , and the

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<sup>22</sup>Univariate GARCH volatility, hereby, refers to the GARCH standard deviation inferred from an autoregression of the real commodity price growth rates.

<sup>23</sup>Several candidates for volatility measures emerge from the literature: historical volatility, realized volatility, implied volatility, and univariate GARCH volatility. Both realized and implied volatility, however, are not applicable to our study as they would require all individual commodities to have price series on a daily basis or daily option markets. Certain commodities, like iron ore for instance, are not traded on commodity exchanges what makes compiling data impossible.

information set  $\Omega_{t-1}$  as follows:

$$\begin{aligned} \partial E(y_{t+k}|\varepsilon_{i,t}, \Omega_{t-1})/\partial \varepsilon_{i,t} &= \partial(\Theta_k B^{-1} \varepsilon_t)/\partial \varepsilon_{i,t} \\ &+ \sum_{\tau=0}^{k-1} \partial\{[\Theta_\tau \Pi_0 (\tilde{F} + \tilde{G})^{k-\tau-1} \tilde{F}] E(\text{vec}(\varepsilon_t \varepsilon_t')|\varepsilon_{i,t}, \Omega_{t-1})\}/\partial \varepsilon_{i,t} \quad (5) \\ &= \Theta_k B^{-1} \iota_0 + \sum_{\tau=0}^{k-1} [\Theta_\tau \Pi_0 (\tilde{F} + \tilde{G})^{k-\tau-1} \tilde{F}] \iota_1. \end{aligned}$$

Thereby,  $\Theta_j$ ,  $j = 1, \dots, k$ , denotes the coefficient matrix at lag  $j$  in the moving average representation of the reduced-form VAR process for  $y_t$  and  $B$  is the structural impact matrix. Furthermore,  $\tilde{F}$  and  $\tilde{G}$  are the coefficient matrices from the multivariate GARCH process and  $\Pi_0 = B^{-1} \Lambda_0$ , where  $\Lambda_0$  denotes the GARCH-in-mean parameter matrix. Finally,  $\iota_0 = \partial \varepsilon_t / \partial \varepsilon_{i,t}$  is a  $2 \times 1$  vector with an impulse of one in the  $i^{\text{th}}$  spot and zeros elsewhere, and  $\iota_1 = \partial E(\text{vec}(\varepsilon_t \varepsilon_t')|\varepsilon_{i,t}, \Omega_{t-1})/\partial \varepsilon_{i,t}$  is a  $4 \times 1$  vector of derivatives with  $2\varepsilon_{i,t}$  in the  $2(i-1) + i$  spot and zeros elsewhere.

Conceptually, the first RHS term,  $\partial(\Theta_k B^{-1} \varepsilon_t)/\partial \varepsilon_{i,t}$ , represents the conventional IRF without any feedback from the GARCH process, whereas the second RHS term can be seen as a correction term that takes the GARCH-in-mean effect  $\Pi_0$  and the underlying dynamics in the second moments (through  $\tilde{F}$  and  $\tilde{G}$ ) into account.

Two things have to be noted. First, Elder (2003) employs a fully vectorized model for the multivariate GARCH process so that the matrices  $\tilde{F}$ ,  $\tilde{G}$ , and  $\Lambda_0$  differ in dimension from our restricted estimates  $F$ ,  $G$ , and  $\Lambda$ . We account for this by setting zeros according to our restrictions when translating  $F$ ,  $G$ , and  $\Lambda$  into  $\tilde{F}$ ,  $\tilde{G}$ , and  $\Lambda_0$ . Second, Elder (2003) derives the above expression for a model with the conditional variance as the in-mean variable. Our model, on the other hand, is specified with the conditional standard deviation in-mean. Hence, the partial derivate in the second RHS term in (5) depends on the level of the conditional variance. To account for this, we linearize the derivative around the average conditional variance, which we also use as the size of the shock.<sup>24</sup>

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<sup>24</sup>Notice that the second RHS term is the partial derivative of  $y_{t+k}$  w.r.t.  $\varepsilon_{i,t}$  taking (only) the effect through the conditional variance into account, i.e.  $\frac{\partial(y_{t+k})}{\partial(h_{t+k})} \frac{\partial(h_{t+k})}{\partial(\varepsilon_{i,t})}$ . Adjusting the partial derivative for the fact that we

use the conditional standard deviation ( $h_{t+k}^{1/2}$ ) in-mean yields the following term  $\frac{\partial(y_{t+k})}{\partial(h_{t+k}^{1/2})} \frac{\partial(h_{t+k}^{1/2})}{\partial(h_{t+k})} \frac{\partial(h_{t+k})}{\partial(\varepsilon_{i,t})}$ , with

$\frac{\partial(h_{t+k}^{1/2})}{\partial(h_{t+k})} = \frac{1}{2} h_{t+k}^{-1/2}$ . Hence, for the computations of the IRFs, we adjust the RHS term by multiplying it with  $\frac{1}{2} \bar{h}^{-1/2}$  in the appropriate position, where we take  $\bar{h}$  to be the average conditional variance.

## D Additional Tables and Figures

Table 4: Share of Commodities in Exports and GDP

	share of comm. in total exp.	share of comm. exp. in GDP		share of comm. in total exp.	share of comm. exp. in GDP
Australia	0,74	0,13	Mexico	0,26	0,07
Brazil	0,53	0,06	New Zealand	0,26	0,07
Canada	0,47	0,14	Norway	0,79	0,30
Chile	0,84	0,30	South Africa	0,46	0,13
Indonesia	0,61	0,16			

Table shows the value share of total commodity exports in total exports and in total GDP. Numbers are author's own calculations based on UNCTAD trade data and Worldbank data for 2008.

Table 5: Estimates of Variance Equations for Baseline Models

First Equation: $h(com)_t = k_1 + F_1 \varepsilon \varepsilon' (com)_{t-1} + G_1 h(com)_{t-1}$ Second Equation: $h(ip)_t = k_2 + F_2 \varepsilon \varepsilon' (ip)_{t-1} + G_2 h(ip)_{t-1}$											
Sample	Lags	F	G	Sample	Lags	F	G	Sample	Lags	F	G
<b>Australia</b>				<b>Brazil</b>				<b>Canada</b>			
74-11	1	0.08 (0.08)	0.86** (0.22)	95-11	1	0.25** (0.10)	0.14 (0.12)	80-11	3	0.20** (0.05)	0.60** (0.11)
		0.36** (0.15)	0.41* (0.24)			0.55** (0.18)	0.00 (-)			0.05* (0.02)	0.92** (0.04)
SIC (VAR):			923.97	SIC (VAR):			2250.73	SIC (VAR):			3083.38
SIC(VAR-MGARCH):			907.10	SIC(VAR-MGARCH):			2198.24	SIC(VAR-MGARCH):			3028.19
<b>Chile</b>				<b>Indonesia</b>				<b>Mexico</b>			
91-11	2	0.24** (0.09)	0.00 (-)	86-11	2	0.36** (0.04)	0.63** (0.05)	80-11	1	0.57** (0.14)	0.00 (-)
		0.07 (0.05)	0.29 (0.28)			0.76** (0.18)	0.00 (-)			0.22** (0.04)	0.75** (0.05)
SIC (VAR):			2794.09	SIC (VAR):			4056.98	SIC (VAR):			3929.14
SIC(VAR-MGARCH):			2785.49	SIC(VAR-MGARCH):			3798.99	SIC(VAR-MGARCH):			3848.79
<b>New Zealand</b>				<b>Norway</b>				<b>South Africa</b>			
77-11	1	0.06 (0.04)	0.73** (0.20)	80-11	3	0.35** (0.10)	0.36** (0.14)	90-11	2	0.35** (0.10)	0.41* (0.19)
		0.65** (0.25)	0.24 (0.21)			0.78** (0.14)	0.00 (-)			0.14* (0.07)	0.06 (0.37)
SIC (VAR):			-1390.93	SIC (VAR):			4595.16	SIC (VAR):			2769.94
SIC(VAR-MGARCH):			-1389.43	SIC(VAR-MGARCH):			4482.89	SIC(VAR-MGARCH):			2752.21

Table shows the estimated autoregressive MGARCH parameters for our baseline models with the lag length based on the Akaike information criterion (constant terms are not reported). Parameters violating the non-negativity constraint necessary in the VECH are restricted to zero. In addition the Schwartz criterion for the VAR-MGARCH-in-mean and a homoscedastic VAR with the same lag length are given.

\* - significance on 10% level, \*\* - significance on 5% level.



Table 6: Estimates of Commodity Price Volatility Coefficient

VAR-Equation: $ip_t = c + \sum_{i=1}^p a_{1,t-i}ip_{t-i} + \sum_{i=1}^p a_{2,t-i}com_{t-i} + \Lambda_{(1,2)}h(com)_t + \varepsilon_t$											
Sample	Lags	Obs	$\Lambda_{(1,2)}$	Sample	Lags	Obs	$\Lambda_{(1,2)}$	Sample	Lags	Obs	$\Lambda_{(1,2)}$
<b>Australia</b>				<b>Brazil</b>				<b>Canada</b>			
74-11	1	150	<b>-0.11*</b> (0.07)	95-11	1	203	0.07 (0.06)	80-11	3	380	<b>-0.18**</b> (0.07)
74-07	1	134	-0.19 (0.35)	03-11	1	107	-0.07 (0.18)	80-07	3	332	<b>-0.40**</b> (0.19)
<b>Chile</b>				<b>Indonesia</b>				<b>Mexico</b>			
91-11	1	250	<b>-0.34*</b> (0.19)	86-11	2	309	<b>-0.10**</b> (0.05)	80-11	1	382	-0.04 (0.02)
91-07	1	202	-0.24 (0.29)	99-11	1	155	<b>-0.25**</b> (0.11)	96-11	1	191	-0.07 (0.07)
<b>New Zealand</b>				<b>Norway</b>				<b>South Africa</b>			
77-11	1	137	0.24 (0.19)	80-11	3	380	<b>-0.29**</b> (0.09)	90-11	2	261	-0.02 (0.10)
77-07	1	121	0.15 (0.60)	80-07	3	332	<b>-0.39**</b> (0.14)	90-07	2	213	0.13 (0.12)

Table shows the estimated parameter measuring the direct impact of conditional commodity price volatility on output. This table reports results with the lag length based on the Schwartz information criterion as a measure of robustness. Values in parentheses are asymptotic standard errors based on inverse of the Hessian.

\* - significance on 10% level, \*\* - significance on 5% level.

Table 7: Estimates of Commodity Price Volatility Coefficient (PPP Exchange Rates)

VAR-Equation: $ip_t = c + \sum_{i=1}^p a_{1,t-i}ip_{t-i} + \sum_{i=1}^p a_{2,t-i}com_{t-i} + \Lambda_{(1,2)}h(com)_t + \varepsilon_t$											
Sample	Lags	Obs	$\Lambda_{(1,2)}$	Sample	Lags	Obs	$\Lambda_{(1,2)}$	Sample	Lags	Obs	$\Lambda_{(1,2)}$
<b>Australia</b>				<b>Brazil</b>				<b>Canada</b>			
74-11	2	150	<b>-0.08**</b> (0.03)	95-11	1	203	0.05 (0.28)	80-11	3	380	<b>-0.20**</b> (0.06)
	4	147	<b>-0.10**</b> (0.03)		5	199	0.06 (0.18)		6	377	<b>-0.20**</b> (0.07)
74-07	1	134	0.01 (0.02)	03-11	1	107	-0.09 (0.30)	80-07	3	332	<b>-0.34**</b> (0.13)
	4	131	0.01 (0.02)		4	104	-0.13 (0.27)		6	329	<b>-0.33**</b> (0.05)
<b>Chile</b>				<b>Indonesia</b>				<b>Mexico</b>			
91-11	1	250	-0.29 (0.21)	86-11	2	309	<b>-0.10**</b> (0.05)	80-11	1	382	<b>-0.14**</b> (0.04)
	3	248	-0.29 (0.22)		3	308	<b>-0.08**</b> (0.03)		2	381	<b>-0.11**</b> (0.04)
91-07	1	202	-0.25 (0.30)	99-11	1	155	<b>-0.25**</b> (0.11)	96-11	1	191	-0.06 (0.04)
	3	200	-0.24 (0.32)		4	152	-0.08 (0.14)		2	190	-0.04 (0.04)
<b>New Zealand</b>				<b>Norway</b>				<b>South Africa</b>			
77-11	1	137	0.30 (0.24)	80-11	3	380	<b>-0.37**</b> (0.07)	91-11	2	249	-0.01 (0.13)
	2	136	-0.03 (0.04)		6	377	<b>-0.44**</b> (0.08)		3	248	-0.03 (0.13)
77-07	1	121	-0.01 (0.03)	80-07	3	332	<b>-0.40**</b> (0.08)	91-07	2	201	-0.20 (0.27)
	2	120	-0.02 (0.04)		6	329	<b>-0.43**</b> (0.07)		3	200	-0.19 (0.28)

Table shows the estimated parameter measuring the direct impact of conditional commodity price volatility on output. Different to our baseline specifications, real commodity price indices are constructed using PPP adjusted real exchange rates. We report estimations with lag length based on the Schwartz information criterion and on the Akaike criterion. Values in parentheses are asymptotic standard errors based on inverse of the Hessian.

\* - significance on 10% level, \*\* - significance on 5% level.

Table 8: Results from ADL models with alternative volatility measures

Estimated Equation: $y_t = \beta_0 + \sum_{i=1}^p \beta_i y_{t-i} + \sum_{i=1}^q \alpha_i x_{t-i} + \sum_{i=1}^r \gamma_i z_{t-i} + \varepsilon_t$ $y_t$ : $\Delta$ industrial production, $x_t$ : $\Delta$ country specific commodity price index, $z_t$ : alternative volatility measure								
GARCH	SD 3	SD 12	GARCH	SD 3	SD 12	GARCH	SD 3	SD 12
<b>Australia</b>			<b>Brazil</b>			<b>Canada</b>		
74-11			95-11			80-11		
-0.13	-0.01	-0.03	-0.01	0.01	-0.07	-1.87**	-0.11**	-0.09**
(-0.79)	(-0.45)	(-1.11)	(-0.03)	(0.25)	(-0.79)	(-2.55)	(-3.54)	(-2.28)
74-07			03-11			80-07		
0.28	-0.01	-0.21**	-0.23	-0.01	0.00	-10.67**	-0.16**	-0.12
(0.36)	(-0.12)	(-2.40)	(-0.47)	(-0.29)	(0.07)	(-2.02)	(-3.06)	(-1.63)
<b>Chile</b>			<b>Indonesia</b>			<b>Mexico</b>		
91-11			86-11			80-11		
-0.06	-0.04	-0.01	-0.32**	-0.06*	-0.07*	-0.21**	-0.07**	-0.05**
(-0.03)	(-0.60)	(-0.10)	(-2.56)	(-1.87)	(-1.80)	(-3.68)	(-5.22)	(-2.99)
91-07			99-11			96-11		
-0.33	-0.06	-0.09	0.27	0.07	-0.01	-0.39*	-0.05**	-0.07*
(-0.11)	(-0.85)	(-0.73)	(0.40)	(1.19)	(-0.04)	(-1.80)	(-2.31)	(-1.74)
<b>New Zealand</b>			<b>Norway</b>			<b>South Africa</b>		
77-11			80-11			90-11		
-0.05	0.07	-0.05	-1.36**	0.04	-0.03	-0.44	-0.06	-0.06
(-0.22)	(1.61)	(-0.73)	(-2.40)	(0.69)	(-0.38)	(-0.65)	(-1.00)	(-0.78)
77-07			80-07			90-07		
-0.03	0.06	-0.02	-1.27**	0.03	-0.01	0.01	0.00	0.05
(-0.12)	(1.43)	(-0.34)	(-1.97)	(-0.48)	(-0.15)	(0.01)	(-0.06)	(0.01)

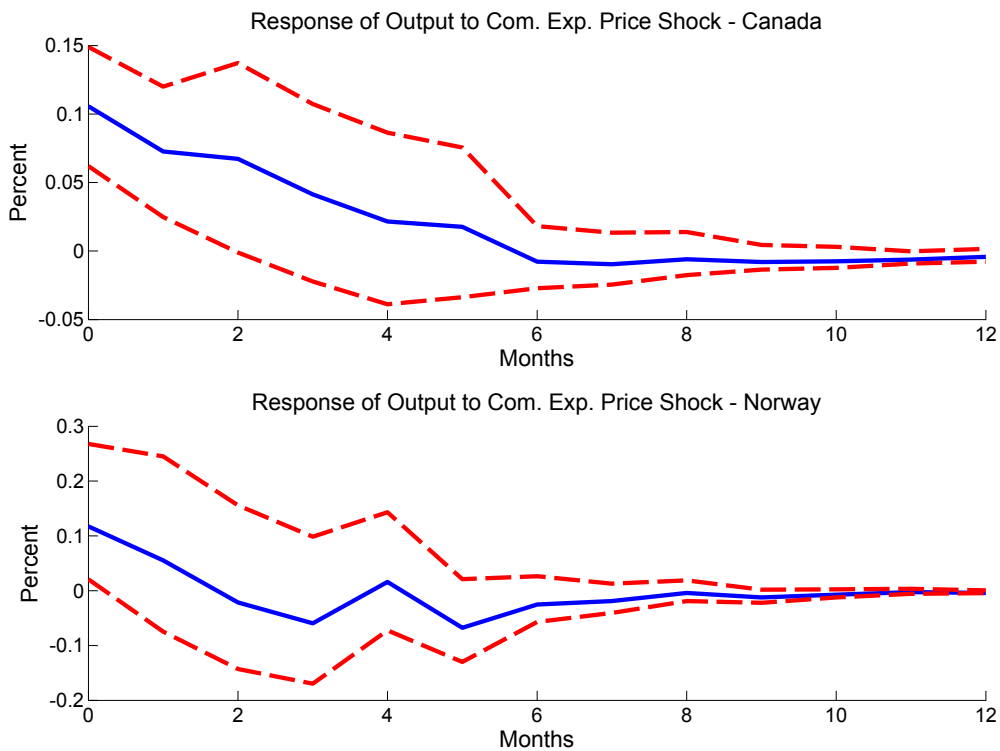
Table displays results from estimations of ADL models with alternative volatility measures.

Univariate GARCH volatility refers to the GARCH standard deviation inferred from an autoregression of the real commodity price growth rates. The other measures are rolling 3-month and 12-month standard deviations of the real commodity price indices.

T-values are reported in parentheses.

\* - significance on 10% level, \*\* - significance on 5% level.

Figure 4: Response Functions with volatility influence - Confidence bands



Note: The blue line displays the response of real output to a one standard deviation real commodity price impulse. It is calculated using the estimated coefficients from the SVAR-MGARCH-in-mean model based on the method developed by Elder (2003) that takes the dynamic impact of volatility on the mean ( $\Lambda$ ) into account. Red dashed lines are 68% confidence intervals calculated by parametric bootstraps of the parameter values (5,000 draws from the underlying Gaussian distributions). As standard bootstrapping procedures commonly used for IRFs cannot be applied in this context, Elder and Serletis (2010) propose to use a parametric bootstrap where parameters are drawn from normal distributions with their respective estimated mean and standard deviation. We follow this suggestion, however, we keep the MGARCH parameters constant to ensure a stationary variance process which guarantees mean reversion.

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