

The model–data–overlap.

A new approach to parameter estimation,
model validation, selection and discrimination

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Contents

1	Introduction	1
2	The overlap – a new approach for model discrimination	7
3	Existing approaches for model discrimination and selection	13
3.1	Parameter estimation and model discrimination for regression models	14
3.2	Model selection	25
3.3	Bayesian analysis	29
3.4	Miscellaneous	37
4	The overlap – illustration and motivation	45
4.1	Motivation and reasoning	46
4.2	Overlap notation	53
4.3	Illustrative model and comparison	54
4.4	Linear case	60
5	Algorithmic challenges	65
5.1	Linear propagation	66
5.2	Sampling and propagation	71
5.3	Nonlinear propagation	77
6	Examples	85
6.1	Linear Initial Value Problems	85
6.2	Biokinetic models	93
6.3	Pharmacokinetics	98
6.4	Michaelis-Menten-Kinetics	103
	Summary	107
A	Calculations	109

Bibliography	113
Eidesstattliche Erklärung	135
Curriculum Vita	137