Part I Structural Restrictions on Singularity Sets