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## Liste der häufig verwendeten Abkürzungen

$A$	skalierte innere Ring-Breite
AE	Arbeits-Elektrode
$B$	potentiostatischer Faktor
	oder phys. Breite des Streifens $[B] = m$
BF	Benjamin-Feir-(Kriterium)
C	Kuspe
$(C_{DL}), \mathcal{C}$	(Doppelschicht-)Kapazität
$D, D_L$	Diffusionskonstante
$D_g$	globale Kopplungskonstante
DL	Doppelschicht
$E_0$	externes Potential
$E_{eq}, \text{Eq}$	Equistabilitätswert von $E_0$
F. A.	Fredholm-Approximation
$F_{AE}$	Fläche der AE $[F_{AE}] = m^2$
FP	Fixpunkt
GE	Gegen-Elektrode
GZ	Grenzzyklus
HB, hb	(homogene) Hopf-Bifurkation
$H_0(x, x')$	Potential-Kopplungsfunktion
$H_B(x, x')$	Gesamt-Kopplungsfunktion
$H_{gal}(x, x')$	galvanostatische Kopplungsfunktion
$H_{2D}(x, x', y, y')$	2d-Kopplungsfunktion
$I_g$	Gesamtstrom $[I_g] = m^2$
KF	Kopplungsfunktion
$L$	äußere Ring-Breite, Scheibenradius oder Streifenlänge $[L] = m$
$\mathcal{R}$	gesamter Widerstand der AE $[\mathcal{R}] = m^{-2}$
RE	Referenz-Elektrode
TP	Target Pattern
a	aktiv-stationäre Lösung
$b$	skalierte Breite des Streifens $b = B/L$
$b_i$	Parameter des kubischen Reaktionsstroms
$c(x, t)$	Konzentration an der Phasengrenze
$\tilde{c}_b$	Bulk-Konzentration
$d$	Dämpfungsdifferenz zwischen 0. und 1. Mode
$f_A = h^{-1}$	geometrischer Beitrag zu $\varrho_{ele}$ beim Ring
$f_b$	Beitrag zu $\varrho_{ele}$ beim Streifen (bei F. A.)

$g_A$	Dämpfungskoeffizient der 1. Mode beim Ring
$h, h(x)$	lokale Funktion von $\Phi_z$
$i_{cap}(x, t)$	kapazitive Stromdichte
$i_{eq}$	Equistabilitäts-Stromdichte, $i_{eq} = i_r(u_{wp})$
$i_r(x, t)$	Reaktionsstromdichte
$i_{mig}(x, t)$	Migrationsstromdichte
$i_m(t)$	mittlere Migrationsstromdichte, $i_m = \langle i_{mig} \rangle$
m	gemischt-stationäre Lösung
p	passiv-stationäre Lösung
$r$	radiale Koordinate
sD	stationäre Domäne
sl	Sattel-Schlaufen-Bifurkation
sn	Sattel-Knoten-Bifurkation
sw	Stehende-Welle-Bifurkation
$u(x, t)$	Doppelschichtaufladung
$u_i^0$	Fixpunkte der Doppelschichtaufladung
$w$	phys. Abstand der GE [ $w] = m$
$x, y$	Koordinaten entlang der AE
$z$	Koordinate senkrecht zur AE
$\tilde{x}, \tilde{y}, \tilde{z}$	nichtskalrierte Koordinaten $x = \tilde{x}/L$
$\beta$	skalierter Abstand der RE
$\gamma$	skalierter Abstand der GE
$\tilde{\delta}$	Diffusionsschichtdicke [ $\tilde{\delta}] = m$
$\epsilon$	Zeitkonstante der zweiten Variable
$\theta$	azimutale Koordinate (beim Ring $x = \theta/2\pi$ )
$\kappa$	Kopplungsstärke $\kappa = \sigma/L$
$\lambda, \mu$	Ableitungen von $i_r$
$\lambda_{wp}$	Ableitung von $i_r$ am Wendepunkt $u_{wp}$
$\varrho^{cusp}$	Kuspenwert des Widerstandes
$\varrho_{ele}$	Elektrolyt-Widerstand
$\varrho_g$	externer Widerstand
$\varrho_{tot}$	(spezifischer) Gesamt-Widerstand
$\sigma$	Leitfähigkeit [ $\sigma] = m$
$\Phi(x, z, t)$	Potential im Elektrolyten
$\Phi_0(x, t)$	Potential an der Phasengrenze $\Phi_0(x) = \Phi(x, z = 0)$
$\Phi_{DL} = u$	Doppelschichtaufladung
$\Phi_{RE}(t)$	Potential an der Referenz-Elektrode
$\Phi_m(t)$	Metall-Potential
$\Phi_z(x, t)$	Potential-Normalableitung an der Phasengrenze