



Article

Insight into Inhibitor Binding in the Eukaryotic Proteasome: Computations of the 20S CP

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Abstract: A combination of molecular dynamics (MD) simulations and computational analyses uncovers structural features that may influence substrate passage and exposure to the active sites within the proteolytic chamber of the 20S proteasome core particle (CP). MD simulations of the CP reveal relaxation dynamics in which the CP slowly contracts over the 54 ns sampling period. MD simulations of the SyringolinA (SylA) inhibitor within the proteolytic *B*₁ ring chamber of the CP indicate that favorable van der Waals and electrostatic interactions account for the predominant association of the inhibitor with the walls of the proteolytic chamber. The time scale required for the inhibitor to travel from the center of the proteolytic chamber to the chamber wall is on the order of 4 ns, accompanied by an average energetic stabilization of approximately -20 kcal/mol.

Keywords: proteasome; core particle (CP); SyringolinA inhibitor; proteolytic; active site; molecular dynamics (MD); simulations; electrostatic interactions

1. Introduction

The 26S proteasome complex, found in eukaryotes as well as prokaryotes, is responsible for a range of biological processes, including protein quality control, cell differentiation, antigen processing, signal transduction, cell cycle control, and apoptosis [1]. Together with ubiquitin, the proteasome is responsible for more than 90% of cell protein degradation [1]. The treatment of many life threatening diseases, including certain types of cancer, is based on the selective and efficient inhibition of the proteasome function [1].

In eukaryotes, the 26S proteasome (drawing its name from its Svedberg (S) sedimentation coefficient as determined by density-gradient centrifugation analysis [2]) is composed of the 20S proteasome core particle (CP) and two 19S capping complexes which have a regulatory function [3]. About 150 Å in height and 110 Å in diameter, the 670-kilodalton 20S CP, or multicatalytic protease complex, consists of four heptameric rings, each containing seven subunits, that are stacked on top of each other to form a hollow cylinder [3]. The *A* rings, comprised of the α subunits, form the outer cylinder rings while the *B*-rings, comprised of the β subunits, form the inner rings (Figure 1A). The α and β subunits of the eukaryotic proteasome differ in sequence, with the structural hallmark of the α subunits being the NH₂-terminal extension of about 35 amino acid residues [3]. The interfaces between the *A* and *B* rings are the gates to the antechambers, where peptide substrates travel to undergo proteolysis [4]. Only three of the seven β subunits contain N-terminal proteolytic active centers, β_1 , β_2 , and β_5 (depicted schematically for the *B*₁ ring in Figure 1B,C), with caspase-like, trypsin-like, and chymotrypsin-like proteolytic activities, respectively [5].

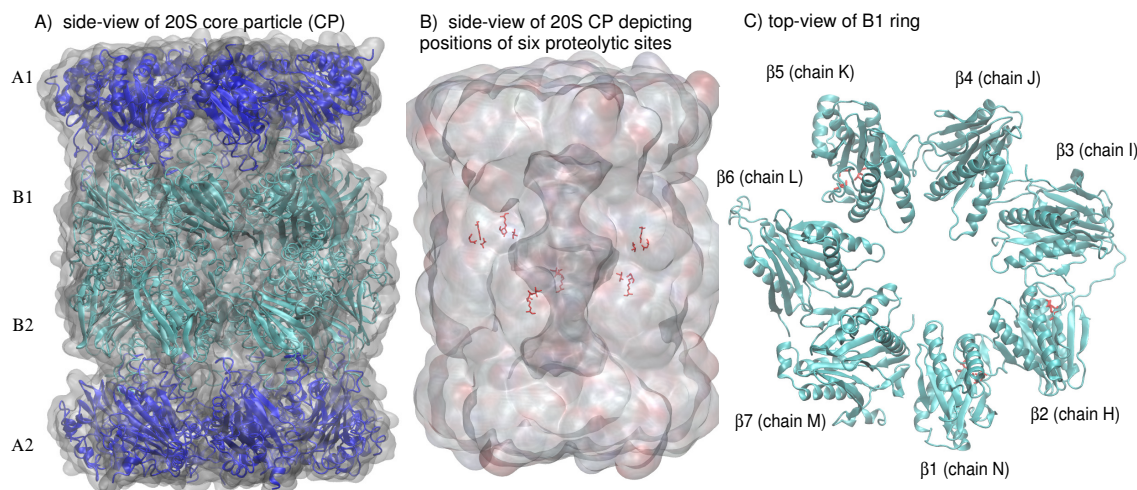


Figure 1. (A) A schematic side-view of the 20S proteasome core particle (CP) depicts the four heptameric rings, each consisting of seven subunits, that are stacked on top of each other to form a hollow cylinder. (B) A side-view of the 20S CP shows the position of the six proteolytic sites located in the two inner *B* rings. (C) A schematic top-view of the *B*₁ ring highlights the ordered arrangement of α -helices and β -sheets in each of the seven subunits; the amino acids (Thr1, Asp17, Lys33) composing the proteolytic sites in β ₁ (chain N), β ₂ (chain H), and β ₅ (chain K) are colored in red (stick representation).

The proteolytic and autocatalytic activities of the 20S proteasome have been well characterized [5]. Using X-ray crystallography and biochemical assays, Huber et al. analyzed the mechanism of β ₁, β ₂, and β ₅ activation. Two sets of catalytic triads were identified: (1) after assembly of the 20S complex, the N-terminal Thr1 of the active site is deprotonated by Lys33 working with Asp17, and (2) Asp166OH, acting with Ser129OH as a proton shuttle, protonates the amine group of Thr1 [5]. The strict conservation of Thr in proteasomes is attributed to the hydrophobic interactions that anchor the C γ of Thr1 with Ala46 (C β), Lys33 (carbon side chain), and Thr3 (C γ) [5]. The positively charged Thr1NH₃⁺ terminus hydrogen bonds to the amide nitrogen of the incoming peptide and stabilizes it (active site residues depicted in Figure 2B), preparing the substrate for endoproteolytic cleavage by Thr1O γ [5].

Several classes of inhibitors exist, including peptide aldehydes, peptide boronates, peptide vinyl sulfones, peptide epoxyketones, and lactacystin and derivatives thereof [1]. Recently, a plant pathogen virulence factor, syringolin A (SylA) was shown to irreversibly inhibit all three catalytic activities of eukaryotic proteasomes [6] (Figure 3). The inhibition mechanism proceeds via a covalent binding of the hydroxy group of the active site amino (N)-terminal Thr1 to the SylA double bond located at the C₄ position [6,7]. Co-crystallization of SylA with the 20S proteasome (2.90 Å resolution) showed binding at all six active sites of the proteasome (pdb structure 2ZCY) [6]. Structural studies have also been carried out on SylB, which differs from SylA by the substitution of the SylA 3,4-dehydrolysine residue with a lysine moiety, to compare selectivity and potency of proteasome inhibition [8]. SylB was found to bind only to subunits β ₂ and β ₅, whereas SylA binds to all three catalytic subunits [8].

Detailed reaction pathways and free energy profiles for the inhibition reaction of the proteasome (catalytic subunit β ₅) have been computed for SylA and another peptide inhibitor, epoxomicin using model systems consisting of the β ₅ and β ₆ subunits [7,9]. Nonetheless, the mechanism that governs the trafficking of substrates from the outer *A* ring annulus to the inner proteolytic chamber of the *B* ring is still not well understood. What forces drive the incoming peptidic substrate to the cavity walls and ultimately to the proteolytic active sites? Experimental and theoretical studies have tried to unravel the complex machinery of the giant proteasome. Magnetization exchange NMR spectroscopy has been used to study the kinetics of the gating mechanism [10]. There, a single *A* ring (180 kDalton) was used as a model to study the *A* ring gate transition. By comparing rates of gate exchange for viscogens of different sizes, the authors demonstrated that the gating event proceeds through very

small step sizes, involving small protein segments, and that water plays a critical role during this process [10]. The gating event is thought to take place over a series of small steps that involve an effective hydrodynamic radius (EHR) that is $<3.5 \text{ \AA}$. [10]. Using Kramers' theory in the strong friction limit [11], the authors determined that the rate constant for the gating event ranges between 600 ms and 40 ms, in the high viscosity limit [10]. One notable finding was that the internal friction forces (originating from the protein) are on the order of or smaller than the viscosity of water at $45 \text{ }^\circ\text{C}$. The authors conclude that the collisions with water molecules are essential for the gating process.

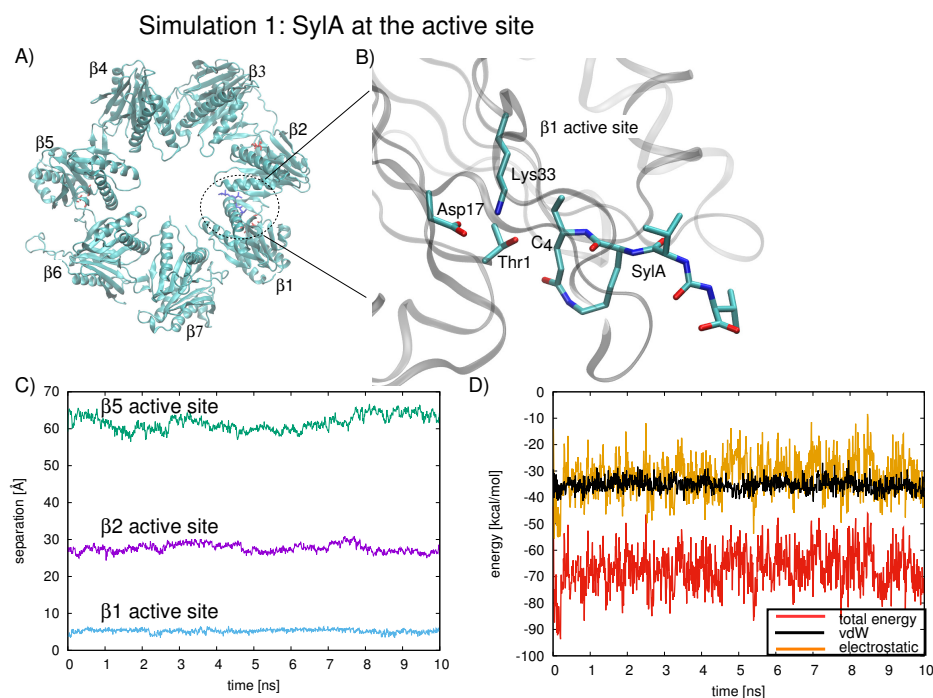


Figure 2. (A) Snapshot of the B_1 ring shown from above, highlighting active site residues (red stick representation) and SylA inhibitor (blue stick representation) at $t = 0.0 \text{ ns}$ (circled in dotted line), as co-crystallized in the proteasome near the active site of the β_1 subunit (PDB ID 2ZCY [6]). (B) Up-close view of the region within the dotted line showing SylA inhibitor at $t = 0.0 \text{ ns}$, as co-crystallized in the proteasome near the active site of the β_1 subunit (PDB ID 2ZCY [6]), is depicted, with residues (Thr1, Asp17, and Lys33) involved in binding the SylA inhibitor labeled. For clarity, SylA and active site nitrogen atoms and oxygen atoms are colored blue and red, respectively; the remainder of the protein is depicted as gray ribbon. (C) The position of the SylA inhibitor during the MD is quantified by the separation between C_4 and Thr1- O^γ of each active site, β_1 (blue line), β_2 (purple line), and β_5 (green line). (D) The total interaction energy between SylA and all seven B_1 subunits energy (red line) can be decomposed into van der Waal's interactions (black line) and electrostatic interactions (orange line). Favorable electrostatic (orange line) and vdW (black line) energies are observed during the duration of the 10 ns simulation, in which the inhibitor is localized at the β_1 active site.

Using NMR spectroscopy, Ruschak et al. investigated the interaction of the 20S CP with three small protein substrates [12]. Using a model system composed of two stacked A rings, the authors conclude that the proteins must unfold to enter the 13 \AA diameter of the ring annulus; once inside the antechamber (cavity of the A rings), the substrates remain unfolded, strongly interacting with the proteasome's cavity walls [12]. The protein conformations are an ensemble of interconverting, unstructured states which is best suited for efficient processing by the proteolytic sites [12].

A recent theoretical investigation used molecular dynamics to study the role of the N-termini tails of the α subunits on the gating mechanism [13]. There, long MD (100 μs) simulations were carried out together with a nine-residue polypeptide (Arg-Pro-Pro-Gly-Phe-Ser-Ala-Phe-Lys) whose sequence

is often used to analyze substrate hydrolysis [13]. The author could show a moderate attraction of the substrate to the inner wall of the antechamber, in agreement with observations of the NMR experiment [12]. These interactions could also influence the substrate's behavior in the proteolytic chamber (B_1 and B_2) [13]. The author also concluded that the dynamics of the N-termini tails were entropically favorable for the translocation of the substrate.

Here, we aim to characterize further the structural features of the 20S proteasome CP that may be responsible for guiding peptide substrates to an active site in the proteolytic chamber of the B rings. On the nanosecond timescale that was considered here, protein side-chain dynamics can be studied [4]. Characterization of the proteasome and its active sites is essential for understanding not only the machinery of the 20S CP but also for the design of effective proteasome inhibitors. We used a combination of molecular modeling, electrostatic energy calculations, and molecular dynamics (MD) to investigate the proteasome with and without the presence of an inhibitor substrate. To study inhibitor dynamics, the B_1 ring was simulated with the SylA inhibitor in the absence of the remaining three CP rings. This “dissection” approach, i.e., studying an isolated ring of the CP, has been verified experimentally and is considered to be a valid approximation of the ring dynamics in the assembled CP [4,10]. In the next section, we will discuss in detail the construction of the models and the computational methods that we used for each of these modes of investigation.

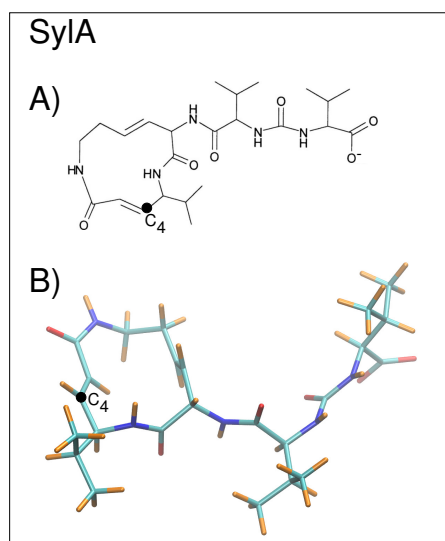


Figure 3. (A) A stick diagram of the SylA inhibitor is shown with C_4 labeled; (B) the non-planar structure of SylA is shown with carbons in cyan, oxygens in red, nitrogens in blue, and hydrogens in orange; C_4 is labeled.

2. Results and Discussion

54 ns MD simulations of the 20S CP proteasome were carried out to investigate the stability and relaxation dynamics of the CP. The relaxation shows moderate (~ 3 Å) root-mean-square deviations (RMSDs) for protein backbone atoms relative to the crystal structure over the 54 ns trajectory (Figure 4A). To analyze the origin of these structural changes, we compared the RMSD deviations relative to the crystal structure for the individual subunits, for the four rings, and for the entire proteasome (Figure 4A). We observe smaller RMSD values (~ 2 – 2.5 Å) for the individual CP rings, as compared to the entire CP structure (purple line in Figure 4A), and for most of the individual ring subunits (α subunits are shown in Figure 4B as an example) RMSD values around 1.5 Å. For subunits α_5 and α'_4 (chains D and R, respectively), the RMSD difference from the backbone atoms of the crystal structure shows the largest (2.5 – 2.9 Å) deviations. The source of these RMSD deviations was examined by analyzing the secondary structure of the α_5 subunit. Less structured loops of the subunit, corresponding to residues 1–12, 46–54, and 115–127, are responsible for raising the subunit's overall

average RMSD (2.5 Å); the remaining residues of the α_5 subunit are more structured and exhibit an overall average RMSD of 1.4 Å.

From these differences in RMSD values, one may conclude that the overall structure of the ring subunits is preserved over the course of the MD simulations while positioning of the subunits of the 20S CP undergoes a conformational change relative to the starting structure. These changes may be viewed as relaxation dynamics, in which the CP slowly contracts, but longer simulation times would be necessary to assess this dynamical behavior definitively. The source of this relaxation dynamics was analyzed by calculating the radius of gyration and the relative position (along the Z axis) of the center of mass (C.O.M.) for each of the four rings (Figure 5A,B). The radius of gyration of the outer rings, A_1 and A_2 , is smaller than that of the inner rings due to the presence of the NH_2 -terminal tails that extend toward the ring center. The A rings exhibit a slight decrease (0.25–0.50 Å) in radius of gyration over the sampling period, and the two inner rings, B_1 and B_2 , with a larger radius of gyration, also show changes in ring compactness. Interestingly, at $t = 54$ ns, the C.O.M. of A_1 , $Z = +63$ Å, is close to its initial position of $Z = +60$ Å (purple line in Figure 5B) while the A_2 C.O.M. position (green line in Figure 5B) shifts nearly 10 Å upward toward B_1 , from $Z = -60$ Å to $Z = -50$ Å. Similarly, B_2 demonstrates a shift of nearly 10 Å upward toward B_1 . The overall result of these ring shifts is a slight compression of the proteasome over the 54 ns relaxation period. Again, longer simulation times are required in order to assess this dynamical behavior. The compression could be a relaxation process or a snapshot of a dynamical “breathing” in which the CP compresses and expands over long times.

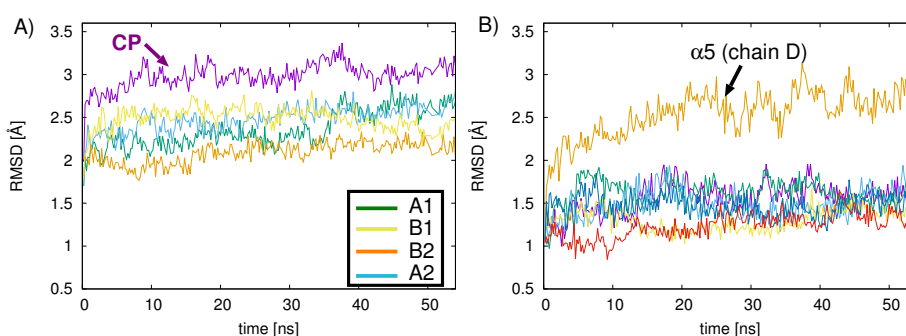


Figure 4. (A) protein The backbone RMSD (Å) relative to the crystal structure is shown over the 54 ns simulation time for the apo 20S CP (purple) and for the four ring systems A_1 (green), B_1 (yellow), B_2 (orange), and A_2 (blue) and (B) for the A_1 subunits: α_1 (chain G) red, α_2 (chain A) purple, α_3 (chain B) green, α_4 (chain C) light blue, α_5 (chain D) orange, α_6 (chain E) yellow, α_7 (chain F) dark blue. Subunit α_5 (chain D) (orange), indicated with the arrow, shows the largest RMS deviations over the simulation time period, arising from less structured loops.

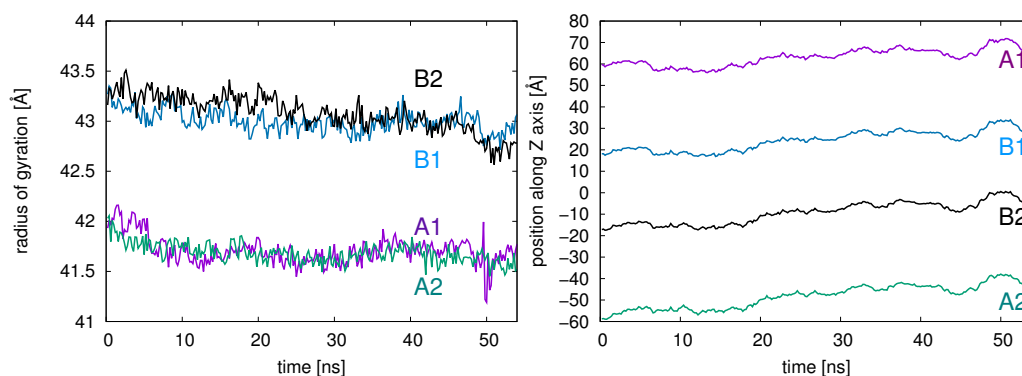


Figure 5. (A) The radius of gyration (Å) and (B) the position along the Z-axis of each ring's C.O.M. is shown for each of the four ring systems A_1 (purple), B_1 (blue), B_2 (black), and A_2 (green) over the 54 ns simulation time.

The stability of the 20S CP was next analyzed by computing the electrostatic energies of all subunits in the four heptameric rings. Figure 6 reports the calculated electrostatic energy for each subunit. In the A_1 ring, the energies vary between -120 kcal/mol and -196 kcal/mol. The largest deviation of these energies occurs between subunits α_2 (chain A) and α_3 (chain B), for which the $\Delta E = E(\alpha_2) - E(\alpha_3) = 76$ kcal/mol. This dip in potential energy is located above the two subunits with the lowest electrostatic energy in the B_1 , subunits β_2 (chain H) and β_3 (chain I), -235 and -234 kcal/mol, respectively. Both subunits (chains H and I) are flanked by subunits whose electrostatic energies are the highest of all seven subunits in the B_1 (chain J is -99 kcal/mol and chain N is -97 kcal/mol). In other words, the potential energy climb from the active site subunits to the left or to the right is approximately 135 kcal/mol (Figure 6). The third active site subunit, β_5 (chain K), has a moderate energy of -111 kcal/mol. A similar pattern is observed in the B_2 ring. Subunit β_7' (chain W) (-220 kcal/mol) is flanked on one side by β_6' (chain X) with a higher electrostatic energy (-96 kcal/mol) and on the other side by β_1' (chain V) with a similar electrostatic potential (-220 kcal/mol). The β_1' (chain V) subunit, containing an active site, is flanked on the other side by a subunit with a much higher electrostatic energy (-93 kcal/mol).

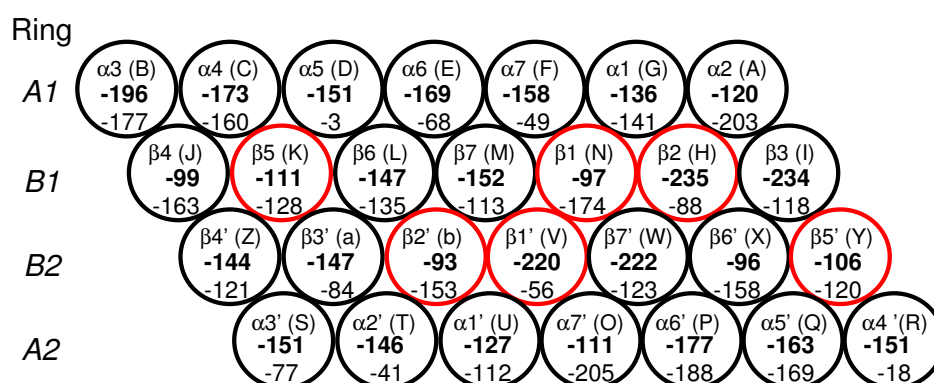


Figure 6. The diagram shows the arrangement of the 28 subunits within the four heptameric rings, A_1 , B_1 , B_2 , and A_2 , of the CP of the 20S proteasome. The subunits containing proteolytic active sites are outlined in red. The chain labels, according to PDB 5CZ4 [5], are listed in parentheses for clarity. Electrostatic energies (kcal/mol) (bold numbers) and solvation binding energies (kcal/mol) are shown for each subunit.

The pattern of electrostatic energy distribution in the outer A_2 ring is quite similar to that of the A_1 ring. The largest deviation between neighboring subunits occurs between α_6' (chain P) and α_7' (chain O), for which the $\Delta E = E(\alpha_6') - E(\alpha_7')$ is 66 kcal/mol. This dip in electrostatic energy is located directly below the subunit β_7' (chain W) with the lowest electrostatic energy in the B_2 ring.

To check whether electrostatic energy distributions may be related to the binding strength of the subunits within the ring, we calculated the binding solvation energy (Figure 6). The weakest binding energies of all 28 subunits were calculated for α_5 (chain D) (-3 kcal/mol), and α_4' (chain R) (-18 kcal/mol) (see Section 3.4). These two subunits, α_5 and α_4' , are both positioned above/below the β_5 (chain K) and β_5' (chain Q) subunits containing an active site (see subunit arrangement in Figure 6). Interestingly, the α_5 and α_4' subunits in the original PDB were the only subunits missing internal residues. The lack of structural information for these two subunits could reflect the weak binding strength or a region of relatively high mobility, perhaps due to gateways of substrate entry/exist.

In the A rings, the strongest binding energies were calculated for α_2 (chain A) and α_7' (-203 kcal/mol and -205 kcal/mol, respectively). The strongest binding energies in the B rings are β_4 (chain J) and β_6' (chain X) (-163 kcal/mol and -158 kcal/mol). Both subunits are flanked on the side and above or below by a subunit containing an active site (see Figure 6). One can speculate that strongly bound subunits may be responsible for maintaining the local geometry of the subunits near active site subunits. Of the B rings, the two subunits with the highest average B-factor (Table A1

in Appendix A), β_2 (chain H) and $\beta_{1'}$ (chain V) (both active site-containing subunits), have the weakest binding energy (-88 kcal/mol and -56 kcal/mol, respectively), possibly related to the need for these subunits to be flexible enough to accommodate substrates. Variations in electrostatic energies and binding strengths thus reflect differences in *A* and *B* ring architectures that may lead to dynamical conformational changes important for substrate processing.

Next, we examined the dynamics of the SylA inhibitor inside the proteolytic chamber by carrying out MD simulations of the SylA with the smaller model system, the proteolytic ring B_1 . In the first simulation, at $t = 0$ ns, the inhibitor is localized at the β_1 active site. In the three further independent simulations, at $t = 0$ ns, the inhibitor is located in the ring center. We quantify the average position of SylA with respect to the three active sites throughout the 10 ns simulation as the separation of SylA C_4 (involved in covalent bonding with Thr1- O^γ) from the Thr1- O^γ of each binding site, β_1 , β_2 , and β_5 .

In the first simulation (simulation 1, Figure 2A), at $t = 0$ ns, the inhibitor is localized in the region of the β_1 active site (see Figure 2B for scheme of SylA located at β_1 active site). The inhibitor remains anchored at this position for the duration of the 10 ns simulation (Figure 2C, separation of SylA C_4 from the Thr1- O^γ of β_1 , β_2 , and β_5 shown in blue, green, and purple lines, respectively). The interaction energy between SylA and all seven B_1 subunits was calculated for the 10 ns simulation; the average interaction energy is -67.3 ± 7.5 kcal/mol (Figure 2D, red line). The total interaction energy can be broken down into van der Waal's interactions (Figure 2D, black line) and electrostatic interactions (Figure 2D, orange line), both of which are favorable throughout the 10 ns sampling period, explaining the stability of the inhibitor's position at the active site of β_1 .

Next, to model the scenario in which the inhibitor may migrate from the ring center towards the proteasome wall, three independent trajectories (simulations 2–4) were started for the B_1 +SylA complex in which the initial position of the SylA inhibitor was the center of the ring (Figure 7A–C). Again, the inhibitor position with respect to the three binding sites is quantified by the separation of the SylA C_4 atom from the Thr1- O^γ atom of each binding site, β_1 (blue), β_2 (purple), and β_5 (green), shown in Figure 7.

All three simulations demonstrate that, starting from the ring center at $t = 0$ ns, the inhibitor migrates to a position nearer to the proteasome wall. In other words, SylA is never localized in the ring center, so the probability of being near an active site is increased. However, over the 10 ns sampling time, the inhibitor is never located directly at a binding site, so an affinity with the set of catalytic amino acids cannot be claimed. The simulation showing the closest association between SylA and an active site is simulation 3, for which after 4 ns SylA is located closest to the proteolytic site in subunit β_5 (green line in Figure 7B) and farthest from proteolytic subunits β_1 and β_2 (Figure 7B, blue and purple lines, respectively). This position is maintained throughout the 10 ns simulation (snapshot in right-hand panel of Figure 7B).

In simulation 2, around 4 ns the inhibitor (shown in dark blue stick representation in Figure 7A) has traveled to subunit β_6 , adjacent to the proteolytic site at β_5 , with a separation ca. 40 Å between SylA C_4 and Thr1- O^γ of β_5 (Figure 7A, green line). The separation from the proteolytic sites in subunits β_1 (Figure 7A, blue line) and β_2 (Figure 7A, purple line) is around 60 Å. At 10 ns (snapshot in right-hand panel of Figure 7A), the inhibitor is still located close to subunit β_6 .

In simulation 4 (Figure 7C), the inhibitor visits regions near β_4 , nearly equidistant (ca. 36 Å at $t = 10$ ns) from β_2 and β_5 , with some fluctuations in position (Figure 7C, purple and green lines, respectively); at $t = 10$ ns, SylA is farthest (ca. 48 Å) from β_1 (Figure 7C, blue line) and located at the interface between β_3 and β_4 . This region is characterized by a large gradient in electrostatic energy (see Figure 6) which may attract the inhibitor. To check the forces driving the inhibitor's dynamical position, the interaction energy between the SylA inhibitor and all seven B_1 subunits was calculated for each of the three trajectories (shown in Figure 8A–C).

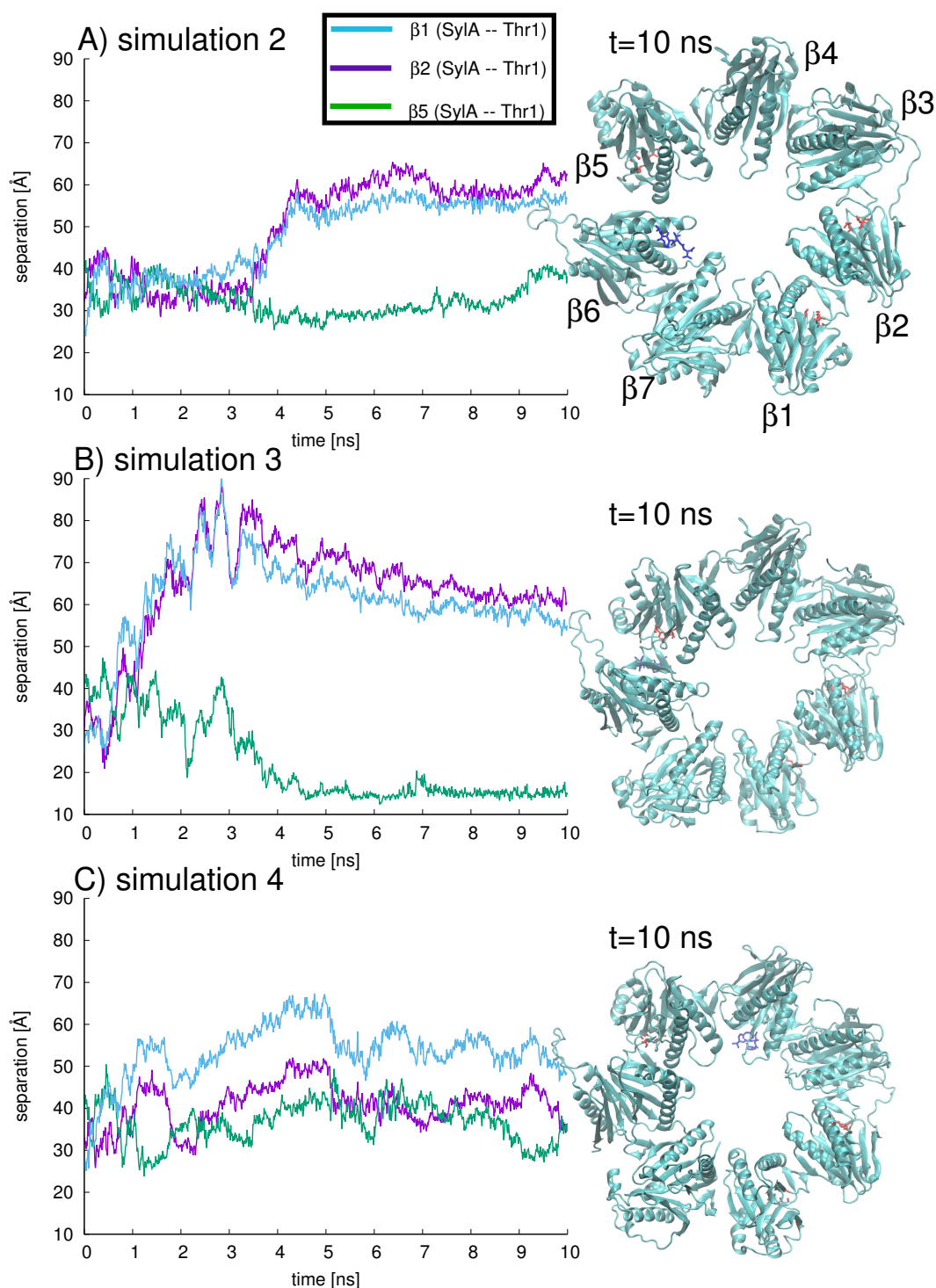


Figure 7. Three independent simulations, labeled simulation 2, 3, and 4 (shown in figures A–C, respectively), were carried out with the B_1 +SylA complex over 10 ns. In each simulation, the SyLA position with respect to the three binding sites is quantified by the separation of SyLA C_4 from the Thr1- O^γ of β_1 (blue), β_2 (purple), and β_5 (green). Snapshots of the SyLA inhibitor (dark blue) inside the B_1 ring (active sites depicted in red) are shown for each simulation at $t = 10$ ns.

For all simulations, an energetic stabilization is observed as the inhibitor moves from the center of the ring to the ring walls. In simulation 2, SyLA is in close proximity to the protein chains of β_6 , leading to the favorable electrostatic and van der Waals energies (Figure 8A, orange and black lines, respectively). Simulation 2 briefly exhibits the lowest total energy, close to -100 kcal/mol

(Figure 8A, red line), near 9.6 ns, followed by simulation 4 with frequent low energy (ca. -50 kcal/mol) configurations (Figure 8C, red line). Simulation 3 shows one low energy configuration (-50 kcal/mol around 8 ns) (Figure 8B, red line). In general, the electrostatic interactions (Figure 8A–C, orange lines) comprise the dominant energetic contribution to the stabilizing energy between inhibitor and ring subunits, while the van der Waals energies (Figure 8A–C, black lines) provide relatively moderate energetic stabilization.

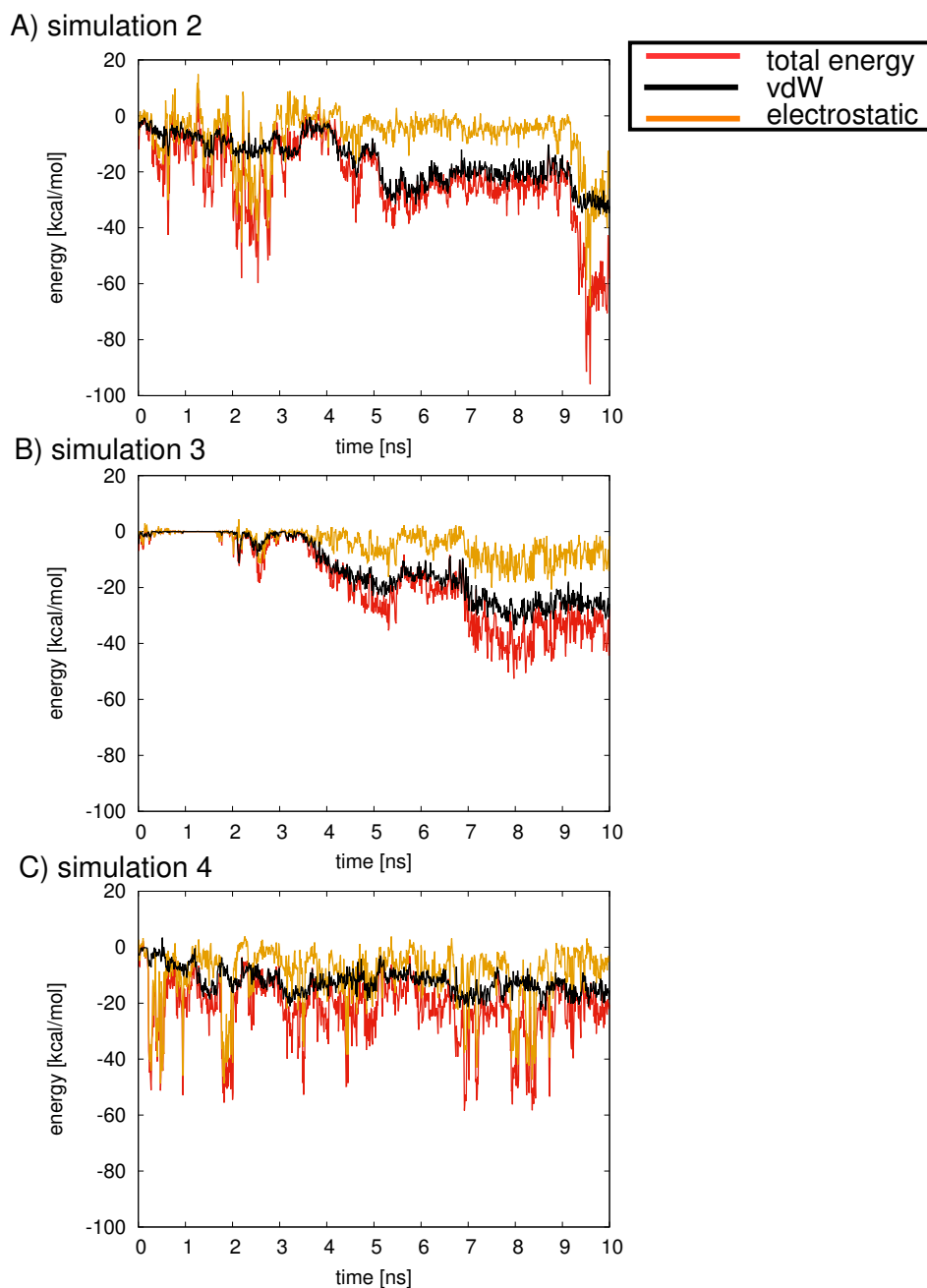


Figure 8. For each of the three independent simulations discussed in Figure 7, labeled simulation 2, 3, and 4 (shown in figures A, B, and C, respectively), the interaction energy [kcal/mol] (red) of SylA with all seven B_1 subunits was calculated over the length of the trajectory. A breakdown of the energies into van der Waals (black) and electrostatic (orange) components is shown.

One can compare the energetics of simulations 2–4 over the 10 ns sampling period to those observed in simulation 1, in which SylA is located at the active site of β_1 (Figure 2D). In simulation 2,

the average interaction energy of SylA with the protein subunits is only -23.0 ± 14.8 kcal/mol (compare with -67.3 ± 7.5 kcal/mol found in simulation 1). For simulations 3 and 4, average SylA+B₁ interaction energies of -17.9 ± 14.7 kcal/mol and -22.1 ± 10.9 kcal/mol, respectively, are calculated over the $t = 10$ ns sampling period. Thus, an energetic stabilization is observed as the inhibitor migrates from the ring center to the walls of the proteolytic chamber. Nonetheless, the chemical environment that is realized when SylA is positioned at an active site, as in simulation 1, is not observed in simulations 2–4, reflected in the less favorable electrostatic and van der Waals interactions. Longer sampling may be required to observe the migration of the inhibitor to an active site position. Also, the electrostatic environment of the model system of B₁ may not sufficiently reproduce that of the double B ring system, which in turn influences the dynamical behavior of the inhibitor inside the proteolytic chamber.

3. Methods

3.1. Construction of Models

The 20S proteasome CP was modeled using the PDB 5CZ4 structure (2.30 Å resolution) [5]. The structure consists of 28 subunits; A₁ (1-7), B₁ (1-7), A₂ (1-7), and B₂ (1-7). Here, the two outer rings will be given the notation A₁ and A₂; the inner two rings will be denoted as B₁ and B₂. The subunits of the outer rings will accordingly be denoted with lowercase α while the subunits of the inner rings, B₁ and B₂, are denoted with β . The 28 subunits have corresponding chain labels, as assigned in the PDB [5], A–Z and a and b; these help further distinguish them, and they are listed in Table A1 for clarity [5].

The arrangement and labeling of the subunits in A₁ and B₁ of the proteasome is counterclockwise with respect to the arrangement in A₂ and B₂ (Figure 6). In chains D and R in the B₁ and B₂ rings, respectively, internal residues were missing (residues 118–124) so these were constructed in silico using CHARMM [14] and geometry optimized using 50 steepest descent (SD), followed by 100 adopted basis Newton-Raphson (ABNR) energy minimization steps. Hydrogen atoms were added using H-build from CHARMM [14]. The N-termini of each subunit was capped with a NH₃⁺ group and the C-termini were capped with a COO⁻. In addition, eight magnesium ions, two chlorine atoms, and 1520 water molecules, as found in the crystal structure, were included in the model, yielding a total of 103,063 atoms. All water molecules were modeled using TIP3 water parameters [15].

As a smaller model system, only the B₁ ring was considered together with the syringolin inhibitor, SylA. Two starting structures were prepared: (1) the inhibitor located at the binding site in subunit β_1 (corresponding to chain N) and (2) the inhibitor located in the center of the B₁ ring. Structure 1 was constructed as follows. The lower-resolution PDB structure containing the co-crystallized inhibitor (2ZCY [6]) was superimposed on the higher-resolution apo 5CZ4 structure [5] and the coordinates of the atoms belonging to SylA located at the β_1 subunit (chain N) were saved. The model was then constructed by merging the coordinates of the 20S CP from 5CZ4 with the SylA coordinates from 2ZCY. After modeling, any close contact (2.5 Å) water interactions were removed (47 close-contact waters), resulting in a total of 103,131 atoms. Additional close contacts were initially relaxed using 50 steepest descent (SD), followed by 50 ABNR energy minimization steps resulting in a 0.59 Å RMSD from the crystal protein backbone atoms. To construct structure 2, the inhibitor was positioned in the center of the B₁ ring. This position is assumed to be a non-biased starting position. Since the ring opening is on the order of 13 Å, [10] the substrate could pass through the center of the cylinder annulus, such that it arrives in approximately the center of the proteolytic chamber of the B₁ ring. As modeled, the initial distance from the C₄ of SylA (see Figure 3 for atom labels) to Thr1-O^γ in each of the three active sites in β_1 , β_2 , and β_5 is approximately 27 Å, 34 Å, and 40 Å, respectively. For both models 1 and 2, any water molecule from the 5CZ4 PDB structure that was overlapping with the SylA molecule was deleted. In the case of structure 1, with SylA near the active site, modeling resulted in the deletion of 49 overlapping waters. In the case of structure 2, with SylA in the center of the ring, very few crystal

structure water molecules are contained in this region so only seven overlapping water molecules were removed.

3.2. Potential Energy Function and Energy Minimization

The protein system was treated using the CHARMM36 parameter set for the protein [16,17] and the TIP3P model for water molecules [15]. For the syringolin inhibitor SylA, initial CHARMM parameters for the SylA were generated with the CHARMM General Force Field (CGenFF) (version 1.0.0) [18]. Next, the charges of the heteroatoms atoms (N and O) were optimized in the following manner. At each of the twelve hetero sites (Figure 3), an individual water molecule was constructed such that a colinear hydrogen bond was formed between the water molecule's oxygen and the heteroatom. The resulting hydrogen bond energy and bond length were calculated [HF/6-31g* with a gradient tolerance of 0.00000001 kcal/mol/Å] with the GAMESS suite in CHARMM [19,20]. The resulting set of charges was then used to recalculate the charges for the entire molecule. The final set of SylA atomic charges, corresponding to atoms as shown in Figure A1, is listed in Table A2. Energy minimization was performed using the ABNR routine in CHARMM [14].

3.3. Molecular Dynamics

54 ns relaxation molecular dynamics were carried out for the 20S CP. The cylindrical structure as modeled with water molecules from the crystal structure, was aligned with the ring centers along the Z-axis and placed in a rectangular box ($175 \times 175 \times 202 \text{ \AA}^3$) containing explicit water molecules (481902 total number of atoms, 126385 TIP3 water molecules [15]).

MD simulations were performed with the SylA inhibitor present using the B_1 ring as a model system for the proteasome. The ring, as modeled with inhibitor and water molecules from the crystal structure, was aligned with the Z-axis in the ring center normal to the ring plane and placed in a rectangular box ($150 \times 150 \times 100 \text{ \AA}^3$) containing approximately 71,300 explicit TIP3 water molecules [15]. For structure 2, in which the inhibitor was positioned in the center of the B_1 ring, three independent simulations were carried out, each 10 ns in length.

To simulate a continuous system, periodic boundary conditions were applied. Electrostatic interactions were summed with the Particle Mesh Ewald method [21] ($\sim 1.5 \text{ \AA}$ grid point spacing). The MD simulations used an integration time step of 2 fs and a non-bonded cutoff of 16.0 Å. The temperature (310 K) was controlled using Langevin dynamics, with a collision frequency of 20 ps^{-1} and isotropic position scaling to maintain pressure (1 atm). The SHAKE algorithm was used to constrain all bonds to hydrogen atoms [22]. Heuristic testing was performed at each time step to evaluate whether the non-bonded pair list should be updated.

3.4. Electrostatic Energy Calculations

The electrostatic energy of each of the 28 protease ring subunits was determined numerically by solving the linearized Poisson-Boltzmann equation (LPBE) using the Adapted Poisson-Boltzmann Solver (APBS) [23]. The calculation of electrostatic energies depends first and foremost on the quality of the molecular structure that is being treated [24]. For a particular titration state, the atomic charges and radii are assigned according to the selected force field. Here, the CHARMM22 force field was used, including grid-based energy correction map (named CMAP) terms for protein backbone Φ, Ψ dihedral angles and side-chain torsion potentials [17]. Assuming the structure of the biological system is reliable, solving the LPBE relies on the discretization of the PB equation and determining the electrostatic potential on a grid. The grid spacing, which can affect the solution of the LPBE, is chosen to maximize the resolution across the system of interest. Here the proteolytic ring has approximate dimensions of $110 \text{ \AA} \times 110 \text{ \AA} \times 50 \text{ \AA}$. The number of grid points in the $\{x, y, z\}$ dimensions for each calculation was 417, 449, and 225, respectively, resulting in grid spacings of 0.26 Å, 0.24 Å, and 0.22 Å, in the $\{x, y, z\}$ directions, respectively. In comparison, the 30S small ribosomal subunit (containing 88,000 atoms) filling a box of dimension 200 \AA^3 was treated using the APBS method with a resolution of 0.41 Å [23].

APBS relies on a 10^{-6} error tolerance in the calculated potential. This tolerance has been observed to give good accuracy in APBS calculated energies; nonetheless, a comparison of electrostatic energies calculated using the same methodology typically results in the most meaningful values [23].

Each of the four rings was analyzed separately. Each ring was treated with the dielectric constant of the solvent set to $\epsilon = 80$ and inside the protease volume to $\epsilon = 4$. The choice of $\epsilon = 4$ for inside the protein volume has demonstrated reasonably good agreement with experiments while also accounting for polarization and small backbone fluctuations [23,25,26]. The electrostatic potential experienced by each ring subunit was calculated as follows: for the arrangement of six of the seven ring units, the potential was tabulated by summing over all charges while the charges of the seventh subunit were set to 0. The electrostatic potential energy of the seventh subunit was calculated as a product of its charges with the electric field generated by the remaining six ring subunits. This procedure was repeated seven times within one ring. In total, 28 calculations were carried out, one for each CP ring subunit.

3.5. Solvation Binding Energy Calculations

To estimate the solvation binding energy of each ring subunit, the components of the standard thermodynamic energy cycle were calculated for each subunit according to the scheme in Figure 9. The term $\Delta G1$ is the free energy difference, in an environment with a homogeneous dielectric constant ($\epsilon = 4$), between the product (ring and with subunit separated) and the reactant (complete ring). $\Delta G2$ and $\Delta G4$ refer to the free energy difference gained from moving the solute from an environment with a homogeneous dielectric constant ($\epsilon = 4$, $\epsilon = 4$) to a heterogeneous dielectric environment ($\epsilon = 4$ for the solute, $\epsilon = 80$ for the solvent). The binding energy, $-\Delta G3$, is then calculated from $\Delta G3 = \Delta G1 + \Delta G2 - \Delta G4$.

As for the electrostatic energy calculations, each of the four heptameric rings was analyzed separately. Therefore, the thermodynamic cycle in Figure 9 was calculated for each of the seven subunits in each heptameric ring, resulting in a total of 28 sets of calculations. $\Delta G4$ and $\Delta G2$ were determined by solving the linearized Poisson-Boltzmann equation using the Adapted Poisson-Boltzmann Solver (APBS) [23]. Each ring (aligned with the ring center along the Z-axis) was treated with the same number of grid points: 417, 449, and 225 for the $\{x,y,z\}$ directions, respectively. $\Delta G1$ was calculated using CHARMM [14].

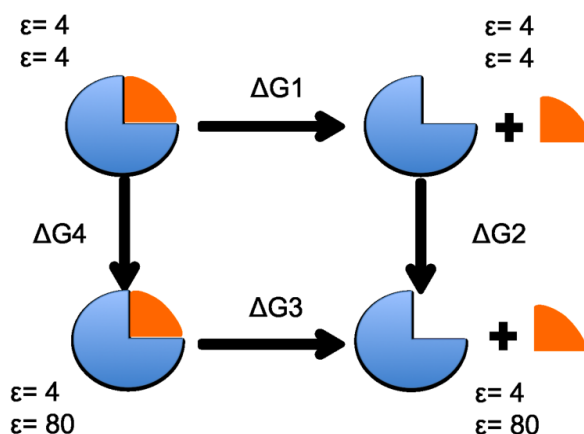


Figure 9. The thermodynamic cycle depicts the steps involved in the calculation of binding free energy of a protein subunit (orange) in the environment of a protein complex (blue).

4. Conclusions

As the delivery of substrates to the active sites in the 20S CP is ATP-independent, the process must be energetically favorable. The forces guiding substrates from the CP's outer A rings to the inner proteolytic chambers arise from the molecular architecture of the subunit arrangement and

from the interaction of the substrate with the CP subunits. Here, we present the results of 54 ns MD simulations of the 20S CP and of the smaller model system, the proteolytic B_1 ring, with the SylA inhibitor. Over the sampled time, the CP demonstrates dynamical contraction behavior, evidenced by RMS deviations, and analysis of A and B ring electrostatics and solvation binding energies indicate variations within the four heptameric rings that may be one source of these conformational changes. Nonetheless, extending the simulation time is necessary to determine whether these changes are due to relaxation or to a “breathing” motion.

Electrostatic energy calculations have located specific regions within the individual rings, for example between β_1 and β_2 of the B_1 ring, that are characterized by a high electrostatic energy gradient. Further analyses of the electrostatic and binding energies of the individual ring subunits reveal variations within the subunits of each ring. These variations may indicate dynamical mobility of the proteasome CP that accommodates substrates in regions containing the catalytically active centers. Here, we have not considered the possibility of non-standard protonation states of titratable residues. As protonation patterns may affect calculated electrostatic properties, future studies should include a comprehensive review of assigned protonation states.

To carry out simulations with SylA, we have computed and parametrized SylA charges. MD simulations of the SylA inhibitor with the smaller proteasome model, the B_1 ring, provide insight into the source of dynamical behavior of the inhibitor. In the first simulation, at $t = 0$ ns, SylA is located at the active site of β_1 , and it remains at its initial position throughout the 10 ns trajectory. In simulations 2–4, in which SylA at $t = 0$ ns was simulated in the center of the ring, an overall stabilization due to electrostatic and vdW energies is observed as the inhibitor migrates toward the proteasome wall. This migration occurs on a time scale of approximately 4 ns. Close proximity to protein chains, regardless of the presence of an active site, is responsible for stabilizing the inhibitor position through favorable electrostatic and van der Waals energies between SylA and the ring subunits.

In the current study, we considered two scenarios for the B_1 ring, namely (1) at $t = 0$ ns, the SylA inhibitor is located at the β_1 active site and (2) at $t = 0$ ns, SylA is located in the center of the ring. In future simulations, additional studies should examine the interaction of SylA with the other two catalytic sites, i.e., at $t = 0$ ns SylA is located directly at either the β_2 or β_5 active site. In addition, the scenario in which all three active sites are occupied with SylA should be examined. The presence of more than one inhibitor in the proteolytic chamber likely increases the probability that the inhibitors spend time near an active site.

The “dissection” approach—studying a single ring of the CP—has been used here in the investigation of inhibitor dynamics. In the future, larger model systems, for example in which both catalytic rings B_1 and B_2 are simulated together, may provide us with more insight into the behavior of inhibitor dynamics within the rings. Extending the duration of MD simulations would also provide us with further insight into large-scale conformational changes in the CP structure, as well as substrate behavior inside the proteolytic chamber. Here, using nanosecond simulations of a single proteolytic ring, we have analyzed the forces driving substrate dynamics, a necessary first step for engineering proteasome inhibitors.

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Conflicts of Interest: The authors declare no conflict of interest.

Abbreviations

The following abbreviations are used in this manuscript:

NPC	Niemann-Pick type C
NPC1	NPC protein 1
NPC2	NPC protein 2
MD	Molecular dynamics
TMD	Targeted molecular dynamics
NTD	N-terminal domain
MLD	Middle luminal domain
CTD	C-terminal domain

Appendix A

Table A1. Electrostatic potential energy, binding energy (each given in [kcal/mol]), and average B-factor of each proteasome ring subunit. The corresponding chain symbol (A–Z, a, and b) from the PDB file 5CZ4.pdb is listed in the parentheses after each subunit. For each of the two **B** rings, the three subunits ($\beta_1, \beta_2, \beta_5$) containing the active sites are marked in bold. The table arrangement of rings is according to the spatial arrangement in the proteasome: A_1, B_1, B_2, A_2 .

Ring	Subunit (pdb Label)	Electrostatic Energy	Binding Energy	Average B-Factor
A_1				
	α_1 (G)	−136	−141	52
	α_2 (A)	−120	−203	52
	α_3 (B)	−196	−177	50
	α_4 (C)	−173	−160	58
	α_5 (D)	−151	−3	60
	α_6 (E)	−169	−68	66
	α_7 (F)	−158	−49	61
		Tot: −1102	Tot: −801	Ave: 57
B_1				
	β_1 (N)	−97	−174	46
	β_2 (H)	−235	−88	52
	β_3 (I)	−234	−118	45
	β_4 (J)	−99	−163	49
	β_5 (K)	−111	−128	47
	β_6 (L)	−147	−135	49
	β_7 (M)	−152	−113	49
		Tot: −1075	Tot: −919	Ave: 48
	β'_1 (V)	−220	−56	56
	β'_2 (b)	−93	−153	47
	β'_3 (a)	−147	−84	48
	β'_4 (Z)	−144	−121	49
	β'_5 (Y)	−106	−120	38
	β'_6 (X)	−96	−158	35
	β'_7 (W)	−222	−123	48
		Tot: −1028	Tot: −815	Ave: 46
A_2				
	α'_1 (U)	−127	−112	57
	α'_2 (T)	−146	−41	71
	α'_3 (S)	−151	−77	76
	α'_4 (R)	−151	−18	64
	α'_5 (Q)	−163	−169	78
	α'_6 (P)	−177	−188	59
	α'_7 (O)	−111	−205	62
		Tot: −1026	Tot: −810	Ave: 66

Table A2. SylA charge parameters are listed with heavy atoms in bold; groups are separated.

Atom	Type	Charge
C1	CG2O6	0.202
N1	NG2S1	-0.512
H27	HGP1	0.308
O2	OG2D1	-0.273
C2	CG331	-0.271
H23	HGA3	0.090
H24	HGA3	0.090
H25	HGA3	0.090
C3	CG331	-0.271
H19	HGA3	0.090
H20	HGA3	0.090
H21	HGA3	0.090
C4	CG311	-0.092
H22	HGA1	0.090
N2	NG2S1	-0.828
H28	HGP1	0.490
C7	CG311	0.051
H18	HGA1	0.090
C8	CG311	-0.090
H14	HGA1	0.090
C9	CG331	-0.271
H11	HGA3	0.090
H12	HGA3	0.090
H13	HGA3	0.090
C10	CG331	-0.271
H15	HGA3	0.090
H16	HGA3	0.090
H17	HGA3	0.090
C5	CG2O3	0.620
C6	CG311	0.048
O1	OG2D2	-0.560
O6	OG2D2	-0.560
H26	HGA1	0.099
C11	CG2O1	0.129
O3	OG2D1	-0.140
N3	NG2S1	-0.448
H29	HGP1	0.332
C11	CG2O1	0.129
O3	OG2D1	-0.140
N3	NG2S1	-0.448
H29	HGP1	0.332
C13	CG2O1	0.305
O4	OG2D1	-0.309
N4	NG2S1	-0.339
H30	HGP1	0.233
C12	CG311	0.044
H10	HGA1	0.090

Table A2. Cont.

Atom	Type	Charge
C14	CG311	0.056
H4	HGA1	0.090
C15	CG311	-0.078
H32	HGA1	0.090
C18	CG2DC1	-0.156
H37	HGA4	0.150
C19	CG2DC1	-0.161
H38	HGA4	0.150
C16	CG331	-0.273
H33	HGA3	0.090
H34	HGA3	0.090
H35	HGA3	0.090
C17	CG331	-0.273
H1	HGA3	0.090
H2	HGA3	0.090
H3	HGA3	0.090
C20	CG2O1	0.443
O5	OG2D1	-0.392
N5	NG2S1	-0.522
H31	HGP1	0.312
C21	CG321	-0.011
H5	HGA2	0.090
H6	HGA2	0.090
C22	CG321	-0.184
H7	HGA2	0.090
H8	HGA2	0.090
C23	CG2D1	-0.146
H9	HGA4	0.150
C24	CG2D1	-0.163
H36	HGA4	0.150

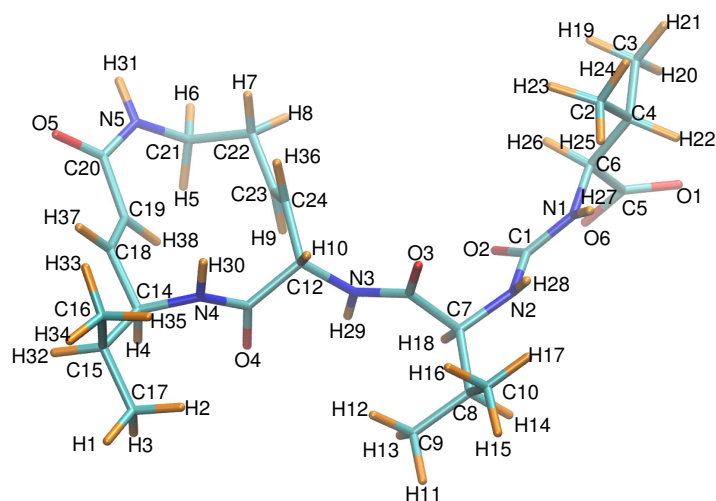


Figure A1. SylA is depicted with each atom labeled according to the numbering scheme of Table A2. Carbons are shown in cyan, oxygens in red, nitrogens in blue, and hydrogens in orange. Note that atom numbering here was only relevant for the charge parametrization procedure and differs from that of, e.g., Ref. [6]; C₁₈ corresponds to C₄.

References

1. Borissenko, L.; Groll, M. 20S proteasome and its inhibitors: Crystallographic knowledge for drug development. *Chem. Rev.* **2007**, *107*, 687–717. [[CrossRef](#)] [[PubMed](#)]
2. Slonczewski, J.; Foster, J.W. *Microbiology: An Evolving Science*; W.W. Norton: New York, NY, USA, 2009.
3. Löwe, J.; Stock, D.; Jap, B.; Zwickl, P.; Baumeister, W.; Huber, R. Crystal structure of the 20S proteasome from the archaeon *T. acidophilum* at 3.4 Å resolution. *Science* **1995**, *268*, 533–539. [[CrossRef](#)] [[PubMed](#)]
4. Sprangers, R.; Kay, L.E. Quantitative dynamics and binding studies of the 20S proteasome by NMR. *Nature* **2007**, *445*, 618–622. [[CrossRef](#)] [[PubMed](#)]
5. Huber, E.M.; Heinemeyer, W.; Li, X.; Arendt, C.S.; Hochstrasser, M.; Groll, M. A unified mechanism for proteolysis and autocatalytic activation in the 20S proteasome. *Nat. Commun.* **2016**, *7*, 10900. [[CrossRef](#)] [[PubMed](#)]
6. Groll, M.; Schellenberg, B.; Bachmann, A.S.; Archer, C.R.; Huber, R.; Powell, T.K.; Lindow, S.; Kaiser, M.; Dudler, R. A plant pathogen virulence factor inhibits the eukaryotic proteasome by a novel mechanism. *Nat. Lett.* **2008**, *452*, 755–759. [[CrossRef](#)] [[PubMed](#)]
7. Wei, D.; Tang, M.; Zhan, C.-G. Fundamental reaction pathway and free energy profile for proteasome inhibition by syringolin A (SylA). *Org. Biomol. Chem.* **2015**, *13*, 6857–6865. [[CrossRef](#)] [[PubMed](#)]
8. Clerc, J.; Groll, M.; Illich, D.J.; Bachmann, A.S.; Huber, R.; Schellenberg, B.; Dudler, R.; Kaiser, M. Synthetic and structural studies on syringolin A and B reveal critical determinants of selectivity and potency of proteasome inhibition. *Proteins* **2009**, *106*, 6507–6512. [[CrossRef](#)] [[PubMed](#)]
9. Wei, D.; Lei, B.; Tang, M.; Zhan, C.-G. Fundamental reaction pathway and free energy profile for inhibition of proteasome by epoxomicin. *J. Am. Chem. Soc.* **2010**, *134*, 10436–10450. [[CrossRef](#)]
10. Latham, M.P.; Sekhar, A.; Kay, L.E. Understanding the mechanism of proteasome 20S core particle gating. *Proc. Nat. Acad. Sci. USA* **2014**, *111*, 5532–5537. [[CrossRef](#)]
11. Kramers, H.A. Brownian motion in a field of force and the diffusion model of chemical reactions. *Physica* **1940**, *7*, 284–304. [[CrossRef](#)]
12. Ruschak, A.M.; Religa, T.L.; Breuer, S.; Witt, S.; Kay, L.E. The proteasome antechamber maintains substrates in an unfolded state. *Nature* **2010**, *467*, 868–871. [[CrossRef](#)] [[PubMed](#)]
13. Ishida, H. Essential function of the N-terminal tails of the proteasome for the gating mechanism revealed by molecular dynamics simulations. *Proteins* **2014**, *82*, 1985–1999. [[CrossRef](#)] [[PubMed](#)]
14. Brooks, B.R.; Bruccoleri, R.E.; Olafson, B.D.; States, D.J.; Swaminathan, S.; Karplus, M. CHARMM: A program for macromolecular energy, minimization, and dynamics calculations. *J. Comput. Chem.* **1983**, *4*, 187–217. [[CrossRef](#)]
15. Jorgensen, W.; Chandrasekhar, J.; Madura, J.; Impey, R.; Klein, M. Comparison of simple potential functions for simulating liquid water. *J. Chem. Phys.* **1983**, *79*, 926–935. [[CrossRef](#)]
16. MacKerell A.D., Jr.; Bashford, D.; Bellott, M.; Dunbrack, R.L., Jr.; Evanseck, J.D.; Field, M.J.; Fischer, S.; Gao, J.; Guo, H.; Ha, S.; et al. All-empirical potential for molecular modeling and dynamics studies of proteins. *J. Phys. Chem. B* **1998**, *102*, 3586–3616. [[CrossRef](#)] [[PubMed](#)]
17. MacKerell, A.D., Jr.; Feig, M.; Brooks, C.L., III. Improved treatment of the protein backbone in empirical force fields. *J. Am. Chem. Soc.* **2004**, *126*, 698–699. [[CrossRef](#)] [[PubMed](#)]
18. Vanommeslaeghe, K.; Hatcher, E.; Acharya, C.; Kundu, S.; Zhong, S.; Shim, J.; Darian, E.; Guvench, O.; Lopes, P.; Vorobyov, I.; et al. CHARMM General Force Field (CGenFF): A force field for drug-like molecules compatible with the CHARMM all-additive biological force fields. *J. Comput. Chem.* **2010**, *31*, 671–690.
19. Schmidt, M.W.; Baldridge, K.K.; Boatz, J.A.; Elbert, S.T.; Gordon, M.S.; Jensen, J.H.; Koseki, S.; Matsunaga, N.; Nguyen, K.A.; Su, S.; et al. General atomic and molecular electronic structure system. *J. Comp. Chem.* **1993**, *14*, 1347–1363. [[CrossRef](#)]
20. Sellers, H. On the interaction of palladium with olefinic systems. *J. Comp. Chem.* **1990**, *11*, 754–763. [[CrossRef](#)]
21. Essmann, U.; Perera, L.; Berkowitz, M.L.; Darden, T.; Lee, H.; Pedersen, L.G. A smooth particle mesh Ewald method. *J. Chem. Phys.* **1995**, *103*, 8577–8593. [[CrossRef](#)]
22. Ryckaert, J.P.; Ciccotti, G.; Berendsen, H.J.C. Numerical integration of the cartesian equations of motion of a system with constraints: molecular dynamics of n-alkanes. *J. Comput. Phys.* **1977**, *23*, 327–341. [[CrossRef](#)]
23. Baker, N.A.; Sept, D.; Joseph, S.; Holst, M.J.; McCammon, J.A. Electrostatics of nanosystems: application to microtubules and the ribosome. *Proc. Nat. Acad. Sci. USA* **2001**, *98*, 10037–10041. [[CrossRef](#)] [[PubMed](#)]

24. Jurrus, E.; Engel, D.; Star, K.; Monson, K.; Brandi, J.; Felber, L.E.; Brookes, D.H.; Wilson, L.; Chen, J.; Liles, K.; et al. Improvements to the APBS biomolecular solvation software suite. *Protein Sci.* **2018**, *27*, 112–128. [[CrossRef](#)] [[PubMed](#)]
25. Schutz, C.N.; Warshel, A. What are the dielectric “constants” of proteins and how to validate electrostatic models? *Proteins* **2001**, *44*, 400–417. [[CrossRef](#)] [[PubMed](#)]
26. Rossini, E.; Knapp, E.-W. Protonation equilibria of transition metal complexes: From model systems toward the Mn-complex in photosystem II. *Coord. Chem. Rev.* **2017**, *345*, 16–30. [[CrossRef](#)]



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