

Algorithms for Comparing Geometric Patterns

(Algorithmen zum Vergleich geometrischer Muster)

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von

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